Name: Date:

### **Chapter 6 Project**

# It's All in the Packaging

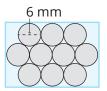
As a member of the People's Pharmaceutical Company's design team, you've been assigned the job of creating part of the packaging for the company's new syringe line. The packages will be sold to retailers in multiples of 10 syringes, and your job is to minimize the packaging for each bundle. Each plastic 1 mL syringe has a diameter of 6 mm and a length of 84 mm.

## Part I - Minimum Surface Area

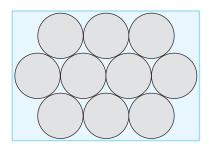
Begin by deciding on the best way to bundle the 10 syringes together; you want to have the smallest surface area in your design. We will try bundling the 10 syringes in a rectangular format and a triangular format. For each possible configuration, calculate the minimum area that would be required to cover the top of that particular bundle of syringes. Be sure to show your calculations. Round your answers to the nearest hundredth.

#### A. Rectangle

The syringes are arranged so that the top of the syringes form the smallest possible rectangle. In order to find the surface area needed to package them, we need to find the area of this rectangle.



1. Let's start with the length *L* of the rectangle. This is the easier of the two measurements to calculate. On the figure below, mark the center of each syringe in the middle row. Then draw a line through the centers that represents the length we need to find.



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**2.** Using the line you just created, determine the general formula for the length *L* of the rectangle in terms of the diameter *d* of each syringe.

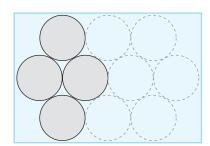
Formula for length of the rectangle: L =

**3.** Now use your formula and the information given about the syringes to calculate the actual length of the rectangle needed to cover the syringes.

Length measurement: *L* = \_\_\_\_\_

Next we'll calculate the width of the rectangle needed. As you are calculating this side, be careful to note that the circles are not sitting directly on top of one another. This allows for the smallest rectangle possible. Let's take a closer look.

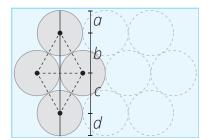
Once again, mark the center of each syringe. By using the radius of each circle, connect the centers of the four syringes shown in such a way that you form two triangles sitting on top of each other. Label each radius r.



**4.** Use either trigonometry or the Pythagorean Theorem to find the height *h* of each triangle you drew based on the radius *r*. Show your work.

Height of each triangle: *h* = \_\_\_\_\_

Now that you have the height of each of your triangles, you are ready to determine the width of the rectangle needed to cover the syringes. On the figure below, we have drawn a line representing the width of the rectangle broken into lengths a, b, c, and d. You are now equipped to find each of these lengths.



**5.** With this in mind, create a formula for the width of rectangle in terms of r.

Formula for Width: W =

**6.** Finally, use the formula you just created and the information given to calculate the actual width of the rectangle covering the syringe bundle.

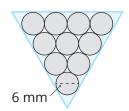
Width measurement: W = \_\_\_\_\_

**7.** You are now ready to calculate the minimum area needed to cover the top of the rectangular bundle of syringes.

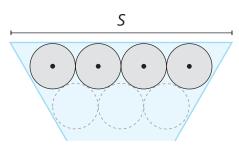
Minimum area = \_\_\_\_\_

#### **B.** Equilateral Triangle

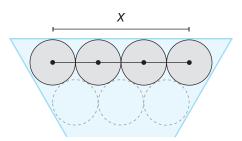
In this configuration, the syringes are arranged so that the top of the syringes form the smallest possible triangle. In order to find the area the triangle covers, we need to know the height of the triangle and the length of one of the sides. Notice that this is an equilateral triangle, so any of the sides will do.



Let's start by finding the length of the sides of the triangle. We've enlarged one of the sides for you in the figure below and indicated the centers of the syringes.

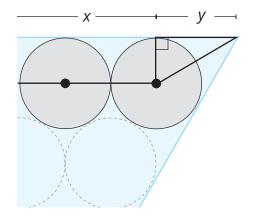


**8.** Notice in the next figure that we can determine part of the length of S by simply using the radius of each syringe. Give the length of x, shown in the figure, in terms of r.



X =			
<i>^</i>			

**9.** Now let's find the remaining bits of side *S*. We'll zoom in closer to the right side. Since the sides are the same it makes no difference which one we calculate. We can create a triangle in the corner using the radius of the circle as our base, as shown. We need to determine the length of *y* in terms of *r*.



This is the same triangle that we found the height of in the first layout design. So the length of y is the same as the earlier height h.

Therefore, *y* = \_\_\_\_\_

10.	Now, determine the total length of a side of the triangle in terms of <i>r</i> .
	Length of a side of the triangle: $S = $
11.	Since this is an equilateral triangle, you can now use the Pythagorean Theorem to find the height of the triangle. Round your answer to the nearest hundredth. Show your work.
	Height of triangle: $H = $
12.	Using the lengths of the sides and height of the triangle, calculate the minimum area needed to cover the top of the triangular bundle.
	Minimum area =
13.	Which configuration in Part I requires the smaller area to cover the top of a bundle of 10 syringes?
Pa	art II - Packaging
14.	For each bundle configuration, calculate the minimum total surface area of a three-dimensional package needed for the 10 syringes. Show your calculations.
	a. Rectangle:
	<b>b.</b> Triangle:

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- **15.** Which of the configurations would you recommend to the People's Pharmaceutical Company design team and why?

## Part III - For Consideration

**16.** Suppose you changed the diameter of the syringes. Would the most efficient packaging stay the same? Why or why not?

**17.** Consider other configurations for the bundles. Can you find a way to package them so that it uses less surface area? Show your work.