

Because the  $y$ -intercept is  $-10$ , the coefficient  $a$  must be chosen so that  $f(0) = -10$ . To make this calculation simpler, begin by multiplying out  $(x - (2 + i))(x - (2 - i))$ .

$$\begin{aligned}(x - (2 + i))(x - (2 - i)) &= (x - 2 - i)(x - 2 + i) \\ &= x^2 - 2x + ix - 2x + 4 - 2i - ix + 2i - i^2 \\ &= x^2 - 2x + \cancel{ix} - 2x + 4 - \cancel{2i} - \cancel{ix} + \cancel{2i} - (-1) \\ &= x^2 - 2x - 2x + 4 + 1 \\ &= x^2 - 4x + 5\end{aligned}$$

Now, substitute  $f(0) = -10$  and solve for  $a$ .

$$\begin{aligned}f(x) &= a(x^2 - 4x + 5)(x + 2) \\ f(0) &= a((0)^2 - 4(0) + 5)((0) + 2) \\ -10 &= a(5)(2) \\ -10 &= 10a \\ a &= -1\end{aligned}$$

Thus, the simplified polynomial function is as follows.

$$\begin{aligned}f(x) &= (-1)(x^2 - 4x + 5)(x + 2) \\ &= -(x^3 + 2x^2 - 4x^2 - 8x + 5x + 10) \\ &= -x^3 + 2x^2 + 3x - 10\end{aligned}$$

## 3.R.9 Exercises

### Concept Check

**True/False.** Determine whether each statement is true or false. If a statement is false, explain how it can be changed so the statement will be true. (**Note:** There may be more than one acceptable change.)

1. Regardless of the value of the exponent, the only possible values for any power of  $i$  are  $i$  and  $-i$ .

2. The product  $\sqrt{a} \cdot \sqrt{b}$  can be rewritten as  $\sqrt{ab}$  as long as  $a$  and  $b$  are real numbers.

3. When  $i$  is squared, the product is 1.

4. The conjugate of  $4 - 5i$  is  $4 + 5i$ .

## Practice

Perform the indicated operations and write each result in standard form.

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5.  $-4i(6 - 7i)$

6.  $(2 + 7i)(6 + i)$

7.  $\frac{5}{4i}$

8.  $\frac{6 + i}{3 - 4i}$

