

CAUTION

Many errors can be made in applying the properties of exponents as a result of forgetting the exact form of the properties. The first column below contains examples of some common errors. The second column contains the corrected statements.

Incorrect	Correct
$x^2x^5 = x^{10}$	$x^2x^5 = x^{2+5} = x^7$
$2^42^3 = 4^7$	$2^42^3 = 2^{4+3} = 2^7$
$(3+4)^2 = 3^2 + 4^2$	$(3+4)^2 = 7^2$
$(x^2+3y)^{-1} = \frac{1}{x^2} + \frac{1}{3y}$	$(x^2+3y)^{-1} = \frac{1}{x^2+3y}$
$(3x)^2 = 3x^2$	$(3x)^2 = 3^2x^2 = 9x^2$
$\frac{x^5}{x^{-2}} = x^3$	$\frac{x^5}{x^{-2}} = x^{5-(-2)} = x^7$

$$\begin{aligned} \text{c. } \frac{(-2x^3y^{-1})^{-3}}{(18x^{-3})^0(xy)^{-2}} &= \frac{(-2)^{-3}x^{-9}y^3}{x^{-2}y^{-2}} \\ &= (-2)^{-3}x^{-9-(-2)}y^{3-(-2)} \\ &= (-2)^{-3}x^{-7}y^5 \\ &= \frac{y^5}{-8x^7} \\ &= -\frac{y^5}{8x^7} \end{aligned}$$

Begin by applying Property 4 in the numerator, Property 5 in the denominator.

Then simplify using Property 2.

Unlike the previous example, Property 3 gets applied at the very end.

$$\begin{aligned} \text{d. } (7xz^{-2})^2(5x^2y)^{-1} &= \frac{49x^2z^{-4}}{5x^2y} \\ &= \frac{49}{5yz^4} \end{aligned}$$

Note that the variable x no longer appears in the expression.

0.3 EXERCISES**PRACTICE**

Simplify each of the following expressions, writing your answer with only positive exponents. See Examples 1 and 2.

- $(-2)^4$
- -2^4
- -3^2
- $(-3)^2$
- $3^2 \cdot 3^2$
- $2^3 \cdot 3^2$
- $4 \cdot 4^2$
- $(-3)^3$
- $\frac{8^2}{4^3}$
- $2^2 \cdot 2^3$
- $\frac{7^4}{7^5}$
- $n^2 \cdot n^5$
- $\frac{x^5}{x^2}$
- $\frac{y^3 \cdot y^8}{y^2}$
- $\frac{3^7}{3^4 s^{-10}}$

Use the properties of exponents to simplify each of the following expressions, writing your answer with only positive exponents. See Examples 1, 2, and 3.

- $\frac{3t^{-2}}{t^3}$
- $-2y^0$
- $\frac{1}{7x^{-5}}$
- $9^0 x^3 y^0$
- $\frac{2n^3}{n^{-5}}$
- $\frac{11^{21}}{11^{19} x^{-7}}$
- $\frac{x^7 y^{-3} z^{12}}{x^{-1} z^9}$
- $\frac{x^4(-x^{-3})}{-y^0}$
- $\frac{s^3}{s^{-2}}$
- $\frac{x^{-1}}{x}$
- $x^{(y^0)} x^9$
- $\frac{x^2 y^{-2}}{x^{-1} y^{-5}}$

28. $\frac{s^5 y^{-5} z^{-11}}{s^8 y^{-7}}$

29. $\frac{2^7 s^{-3}}{2^3}$

30. $\frac{3^{-5}}{(3^{-4} x^5 y^4)^2}$

31. $\frac{-9^0 (x^2 y^{-2})^{-3}}{3x^{-4} y}$

32. $\left[(2x^{-1} z^3)^{-2} \right]^{-1}$

33. $\frac{(3yz^{-2})^0}{3y^2 z}$

34. $(12a^2 - 3b^4)^0$

35. $\frac{3^{-1}}{(3^2 xy^2)^{-2}}$

36. $\left[9m^2 - (2n^2)^3 \right]^{-1}$

37. $\left[(12x^{-6} y^4 z^3)^5 \right]^{-0}$

38. $\frac{x(x^{-2} y^3)^3}{(2x^4)^{-2} y}$

39. $\frac{(-3a)^{-2} (bc^{-2})^{-3}}{a^5 c^4}$

40. $\left[(5m^4 n^{-2})^{-1} \right]^{-2}$

41. $(9x^{-1} z)^2 (2xy^{-3})^{-1}$

42. $(4^{-2} x^5 y^{-3} z^4)^{-2}$

43. $\left[(4a^2 b^{-5})^{-1} \right]^{-3}$

44. $\left[(2^{-3} m^{-6} n^3)^3 \right]^{-1}$

45. $\left[(3^{-1} x^{-1} y)(x^2 y)^{-1} \right]^{-3}$

46. $\left[\frac{100^0 (x^{-1} y^3)^{-1}}{x^2 y} \right]^{-3}$

47. $(5z^6 - (3x^3)^4)^{-1}$

48. $\left[\frac{y^6 (xy^2)^{-3}}{3x^{-3} z} \right]^{-2}$

✎ WRITING & THINKING49. In your own words, explain why $a^0 = 1$.

Apply the definition of integer exponents to demonstrate the following properties.

50. $a^n \cdot a^m = a^{n+m}$

51. $(a^n)^m = a^{nm}$

52. $(ab)^n = a^n b^n$