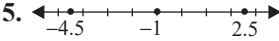
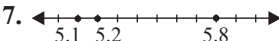

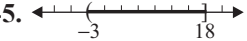
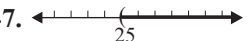


Answer Key

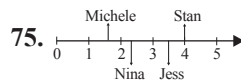
Chapter 1: Fundamental Concepts of Algebra

1.1 Exercises

1. a. $19, 2^5$ b. $19, \frac{0}{15}, 2^5$
 c. $19, \frac{0}{15}, 2^5, -33$
 d. $19, -4.3, \frac{0}{15}, 2^5, -33$
 e. $-\sqrt{3}$ f. all except $\frac{15}{0}$
 g. $\frac{15}{0}$
3. a. $|-16|, \frac{12}{3}, \sqrt{4}$
 b. $|-16|, \frac{12}{3}, 0, \sqrt{4}$
 c. $|-16|, \frac{12}{3}, 0, \sqrt{4}$
 d. all e. none f. all g. none
5. 
7. 
9. $<, \leq$ 11. $<, \leq$ 13. $<, \leq$
 15. $>, \geq$ 17. $>, \geq$
 19. $2a + b > c$ 21. $9 \geq 7$
 23. $x + 5 < 3$ 25. $9 \geq 8$
 27. $\left\{ \begin{array}{l} 3n | n \text{ is an integer} \\ \text{and } -2 \leq n \leq 3 \end{array} \right\}$
 29. $\{n | n \text{ is a prime}\}$
 31. $\left\{ \frac{1}{n} | n \text{ is an odd integer} \right\}$
 33. $(-\infty, 15)$ 35. $(2.5, 3.7]$
 37. $(-\infty, 4)$ 39. $\left(-\frac{1}{2}, \frac{2}{5}\right)$
 41. $[0, \infty)$
 43. 
 45. 
 47. 
 49. 4 51. $\sqrt{5} - \sqrt{3}$
 53. -15 55. 1 57. -1
 59. -12 61. 8 63. 6

65. 11 67. $-\frac{2516}{495}$ 69. 1

71. $\frac{7414}{999}$ 73. $1.08\bar{3}$



77. 20 miles

79. If sugar = s , $\{s | 3 \leq s \leq 4\} = [3, 4]$

If walnuts = w ,

$$\left\{ w \mid \frac{1}{2} \leq w \leq \frac{2}{3} \right\} = \left[\frac{1}{2}, \frac{2}{3} \right]$$

81. Yes, all whole numbers are also integers, but the negative integers are not whole numbers, so not all integers are whole numbers.

1.2 Exercises

1. $3x^2y^3, -2\sqrt{x+y}, 7z$
 3. $-2, \sqrt{x+y}$ 5. 1, 8.5, -14
 7. $\frac{-5x}{2yz}, -8x^5y^3, 6.9z$
 9. $\frac{-5}{2}, \frac{1}{y}, \frac{1}{z}, x$
 11. 20 13. 8
 15. $-\frac{\sqrt{2}}{36} + 2$
 17. 4 19. $58 + 6\pi$
 21. $\frac{-1}{3}$
 23. Commutative
 25. Associative
 27. Associative
 29. Distributive
 31. Commutative
 33. Multiplicative cancellation; $\frac{1}{5}$
 35. Additive cancellation; x
 37. Zero-Factor Property
 39. Multiplicative cancellation; 6
 41. Multiplicative cancellation; $\frac{1}{3}$

43. $\frac{11}{2}$ 45. -10 47. 1
 49. 70 51. $\frac{103}{6}$ 53. $\frac{-144}{5}$
 55. $\frac{37}{2}$ 57. 23.66 59. 1.64
 61. $-\frac{1}{5}(\sqrt{3(3+7)}-5)^3$
 63. $\left(\frac{\sqrt[3]{x-4}}{2}\right)^2$
 65. $(-5, 4]$ 67. $[3, 4]$ 69. $[-\pi, 21)$
 71. $(3, 9]$ 73. \mathbb{Z} 75. \mathbb{Z}
 77. \$66 79. \$102
 81. 2.19 square meters
 83. It is the same number you began with. Explanations may vary.
 85. Answers may vary. (Ex: Please Excuse My Dear Aunt Sally.)

1.3 Exercises

1. 16 3. -9 5. 81
 7. 64 9. 1 11. $\frac{1}{7}$
 13. x^3 15. $27s^{10}$ 17. -2
 19. x^3 21. $121x^7$ 23. x
 25. $\frac{1}{x^2}$ 27. x^3y^3 29. $\frac{16}{s^3}$
 31. $-\frac{y^5}{3x^2}$ 33. $\frac{1}{3y^2z}$ 35. $27x^2y^4$
 37. 1 39. $\frac{c^2}{9a^7b^3}$ 41. $\frac{81y^3z^2}{2x^3}$
 43. $\frac{64a^6}{b^{15}}$ 45. $27x^9$
 47. $\frac{1}{5z^6 - 81x^{12}}$ 49. -0.0000176
 51. 2.1×10^{-7} 53. 5.1×10^3
 55. 312.12 57. 2.587×10^{-8}
 59. 3.1536×10^7
 61. 6.75×10^5 63. 2.605×10^{-7}
 65. 1.2×10^{-9} 67. 50

69. 3.2×10^{-6}
 71. 1.2×10^{13} 75. $7s$
 77. $\pi r^2 h$ 79. 585 m^3
 81. $81\pi d \text{ ft}^3$ 83. $2\pi r^2$

1.4 Exercises

1. -3 3. Not real
 5. -2 7. -5
 9. Not real 11. $-\frac{3}{5}$
 13. $-\frac{1}{2}$ 15. 2
 17. $\frac{2}{5}$ 19. $3|x|$
 21. $\frac{x^2|z|}{2}$ 23. $x^2 y^7 z^3$
 25. $\frac{ab^4}{3c^2}$ 27. $\frac{|x^3|y^2}{2}$
 29. $\frac{y^6 z^5}{2x^7}$ 31. $\frac{\sqrt[3]{36x^2 y^2}}{3y^2}$
 33. $-\sqrt{2} - \sqrt{5}$ 35. $\sqrt{6} + \sqrt{3}$
 37. $\frac{x + \sqrt{2x}}{x-2}$
 39. $\frac{x + 2\sqrt{xy} + y}{x-y}$
 41. $\frac{y-2\sqrt{y}}{y-4}$ 43. $\frac{1}{\sqrt{5}+3}$
 45. $\frac{9-y}{18-6\sqrt{y}}$ 47. $\frac{1}{\sqrt{13}-\sqrt{t}}$
 49. $\frac{6-y}{6+y-2\sqrt{6y}}$
 51. $3x\sqrt[3]{2x}$ 53. Not possible
 55. 0 57. $4z\sqrt[3]{2z}$
 59. 0 61. $(3x^2 - 4)^2$
 63. 27 65. n^2
 67. $\frac{x^{\frac{4}{5}}}{y^{\frac{3}{5}}}$ 69. $\frac{1}{125}$
 71. $y\sqrt[3]{y^2}$ 73. $(ax^2 + by)^{\frac{1}{12}}$
 75. $a^{\frac{15}{4}}$ 77. $x^{\frac{1}{4}}$ 79. $6^{\frac{-1}{3}}$

81. $\sqrt[4]{125}$ 83. $\sqrt[4]{|y|}$ 85. x^3
 87. $\sqrt[6]{16,807}$
 93. $3d^2\sqrt{3}$; 3.326 cm^2
 95. 1651 cm^2 ; no
 97. $2.998 \times 10^8 \text{ m/s}$
 99. Because a root is the same as a fractional exponent.

1.5 Exercises

1. Not a polynomial
 3. Degree 11; polynomial of four terms
 5. Degree 0 monomial
 7. Degree 4 binomial
 9. Degree 2 trinomial
 11. Degree 5 binomial
 13. $-x^{13} + 7x^{11} - 4x^{10} + 9$
 a. 13 b. -1
 15. $2s^6 - 10s^5 + 4s^3$
 a. 6 b. 2
 17. $9y^6 - 3y^5 + y - 2$
 a. 6 b. 9
 19. $\pi z^5 + 8z^2 - 2z + 1$
 a. 5 b. π
 21. $-4x^3 y - 6y - x^2 z$
 23. $x^2 y + xy^2 + 6x - 6y$
 25. $-3ab$
 27. $xy^2 - x^2 y - y$
 29. $3a^3 b^3 + 21a^3 b^2 + 2a^2 b^2 + 14a^2 b - 3ab^3 - 21ab^2$
 31. $3a^2 - 2ab - 8b^2$
 33. $6x^2 + 33xy - 18y^2$
 35. $7y^4 - 34xy^2 - 5x^2$
 37. $6x^3 y^3 - 3x^3 y + 36x^2 y^3 + 4x^2 y^2 - 18x^2 y + 24xy^2$
 39. $9a^2 + 6ab + b^2$
 41. $4x^2 - 9y^2$
 43. $x^2 + 4xy + 4y^2$
 45. $\frac{1}{x^2} - y^2$
47. No; a variable in the denominator is equivalent to a variable with a negative exponent.
 49. a. Yes; degree = 4; leading coefficient = 2; terms = 4
 b. Yes; degree = 3; leading coefficient = 2; terms = 3

1.6 Exercises

1. $m(4mn + 16m^2 + 7)$
 3. $6(a-b^2)$
 5. $2x(x^5 - 7x^2 + 4)$
 7. $(x^3 - y)(x^3 - y - 1)$
 9. $4y^2(3y^4 - 2 - 4y^3)$
 11. $(a^2 + b)(a - b)$
 13. $z(1+z)(1+z^2)$
 15. $(n-2)(x^2 + y)$
 17. $(a-5b)(x+5y)$
 19. $(2x-11)(2x+11)$
 21. $(7a-12b)(7a+12b)$
 23. $(5x^2 y - 3)(5x^2 y + 3)$
 25. $(x-10y)(x^2 + 10xy + 100y^2)$
 27. $(m^2 + 5n^3)(m^4 - 5m^2 n^3 + 25n^6)$
 29. $(3x^2 - 2y^4 z) \times (9x^4 + 6x^2 y^4 z + 4y^8 z^2)$
 31. $(4y^2 z - 3x^4)(4y^2 z + 3x^4)$
 33. $(7y^3 + 3xz^2) \times (49y^6 + 21xy^3 z^2 + 9x^2 z^4)$
 35. $(x+5)(x-3)$
 37. $(x-1)^2$ 39. $(x-2)^2$
 41. $(y+7)^2$
 43. $(x+11)(x+2)$
 45. $(y-8)(y-1)$
 47. $(5a+3)(a-8)$
 49. $(x+6)(5x-3)$
 51. $(16y-9)(y-1)$
 53. $(4a-3)(2a+1)$
 55. $(4y-5)(3y-1)$

57. $2x(2x-1)^{-3}$
 59. $a^{-3}(7a^2-2b)$
 61. $2y^{-5}(5y^3-x)$
 63. $(5x+7)^{\frac{4}{3}}(5x+6)$
 65. $y^{-4}(7y^3+5)$

47. $\frac{5z-3x}{z^2}$ 49. $\frac{x-2}{x+2}$
 51. $\frac{(z^2-11z+54)(z-9)}{(z-2)}$
 53. $\frac{2y^2+5y-4}{y+1}$

3. $[4,17]$ 5. -7 7. 4
 9. -1 11. $-\frac{337}{165}$
 13. $\frac{x^2}{2y}$, $12.1x$, $-\sqrt{y+5}$
 15. $\frac{4\pi}{3}-36$ 17. 51

1.7 Exercises

1. $\frac{2x+1}{x-5}$; $x \neq -3, 5$
 3. $x(x-1)$; $x \neq -3$
 5. $\frac{x+6}{x+5}$; $x \neq -5, 1$
 7. $\frac{1}{x^2-x+1}$; $x \neq -1$
 9. $2x+1$; $x \neq -5$
 11. $2x-3$; $x \neq -7$
 13. $\frac{x^3+9x^2+11x+19}{(x-3)(x+5)}$
 15. $\frac{13x}{(x-3)(x+5)}$
 17. $\frac{x^3+4x^2-7x+18}{(x+3)(x-3)}$
 19. $\frac{x^2+11x+17}{x+3}$
 21. $\frac{x+2}{x-6}$ 23. $y-1$
 25. $(x+2)(2x+3)$
 27. $\frac{y-8}{y+8}$ 29. $5y^2-2y-3$
 31. -6 33. $\frac{x^2+9}{6x-3}$ 35. $\frac{2x^2}{x+1}$
 37. $\frac{s-r}{r^2s+s}$ 39. $\frac{m+n}{mn}$
 41. $\frac{x}{y}$ 43. x^2y^2 45. $\frac{11x}{7y}$

1.8 Exercises

1. $5i$ 3. $-3i\sqrt{3}$ 5. $4i\sqrt{2x}$
 7. $i\sqrt{29}$ 9. $1-3i$ 11. $8-6i$
 13. $-5+6i$ 15. $16-30i$
 17. i 19. -11 21. $40-42i$
 23. -9 25. $1+5i$ 27. $-1-4i$
 29. $7i$ 31. $3+i$ 33. $-i$
 35. $-i$ 37. $10-2i$
 39. $\frac{14}{37}+\frac{10}{37}i$ 41. $\frac{21}{17}-\frac{1}{17}i$
 43. $-5+2i\sqrt{6}$ 45. 8
 47. $-\frac{7}{3}i$ 49. $22+10i\sqrt{3}$
 51. $6+3j$ ohms 53. $11-2j$ ohms

19. Commutative property
 21. Zero-Factor Property
 23. $[5,8]$ 25. $\frac{-t^9}{2s^7}$ 27. $\frac{18y^2}{x^4z^5}$
 29. 6.952×10^7 31. 2.0×10^{-8}
 33. 5 35. $5x^{10}$ 37. $\frac{-4y}{x^3}$
 39. $\frac{2y\sqrt[3]{9x^2y}}{3}$ 41. $-\sqrt{2}-\sqrt{6}$
 43. $3|x|\sqrt{2xy}-2x\sqrt[3]{2xy}$
 45. $\frac{1}{x^4}$
 47. $m^4-5m^3+3m^2+2$
 49. $3x^3-4x^2y^3+3xy-4y^4$
 51. $(x+3)(x-4)$
 53. $(2a+1)(3a-5)$
 55. $(6x^3+y)(6x^3-y)$
 57. $(2x-5y)(x+3)$
 59. $(3x-2y)^{\frac{2}{3}}\left[(3x-2y)^{\frac{2}{3}}-1\right]$

Chapter 1 Project

1. Alex: 81.7; Ashley: 90.3;
 Barron: 81.0; Elizabeth: 83.1;
 Gabe: 90.5; Lynn: 82.4
 3. The final exam contributes a higher percentage of points to the final grade than does the semester project.

61. $\frac{x+3}{x-3}$, $x \neq 0, \pm 3$
 63. $\frac{-2}{x}$ 65. $\frac{b-a}{4a+4b}$
 67. $-x-y$ 69. 3
 71. $5+9i$ 73. $4+i$
 75. $-\frac{7}{25}+\frac{24}{25}i$ 77. $62-16i\sqrt{2}$

Chapter 1 Review Exercises

1. a. 2^3 b. $2^3, 0$
 c. $-\sqrt{4}, 2^3, 0$
 d. All except $\sqrt{17}$
 e. $\sqrt{17}$ f. All

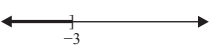
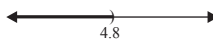

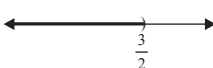
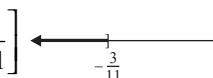
Chapter 2: Equations and Inequalities in One Variable



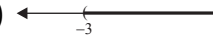
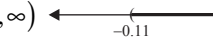
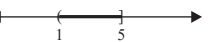

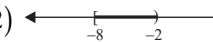
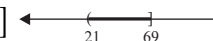

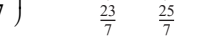
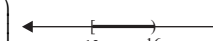
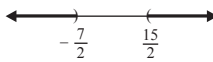
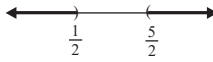
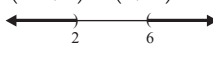





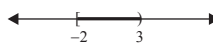
2.1 Exercises

1. $t=-5$ 3. $y=-1$ 5. $w=-3$ 7. \mathbb{R} (Identity) 11. $m=7$ 13. $x=3.7$
 9. \emptyset (Contradiction) 15. $x=1.05$ 17. $y=-5$

19. \mathbb{R} (Identity) 21. \mathbb{R} (Identity)
 23. $x = 3$
 25. \emptyset (Contradiction)
 27. $y = -\frac{1}{3}, -3$ 29. $x = \frac{1}{3}$
 31. $x = -311, 420$
 33. $x = -\frac{4}{5}, 2$
 35. \emptyset (Contradiction)
 37. $x = -2, 2$ 39. $x = 5$
 41. $x = -\frac{1}{2}$ 43. $x = \frac{1}{4}$
 45. $x = \frac{1}{7}$ 47. $r = \frac{C}{2\pi}$
 49. $a = \frac{v^2 - v_0^2}{2x}$
 51. $F = \frac{9}{5}C + 32$
 53. $h = \frac{A - 2lw}{2w + 2l}$
 55. $m = \frac{2K}{v^2}$
 57. $\frac{19}{3}$ hours, or 6 hours and 20 minutes
 59. 13.5 miles 61. \$390
 63. 2 gallons 44%, 1 gallon 50%
 65. 24 child tickets, 15 adult tickets
 67. 7.5%
 69. 26 feet by 26 feet
 71. 53, 55, and 57
 73. 36.4% 75. $x \approx 0.72$
 77. $x \approx 13.11$

2.2 Exercises

1. $\{-9, 3.14, -2.83, 1, -3, 4\}$
 3. $\{-2.83, 1, -3\}$
 5. $(-\infty, -3]$ 
 7. $(-\infty, 4.8)$ 
 9. $(-\infty, 2.25)$ 
 11. $(-\infty, \frac{3}{2})$ 
 13. $(-\infty, -\frac{3}{11}]$ 

15. $(7, \infty)$ 
 17. $(35, \infty)$ 
 19. $(-3, \infty)$ 
 21. $(-0.11, \infty)$ 
 23. $(1, 5]$ 
 25. $(-10, 6]$ 
 27. $[-8, -2]$ 
 29. $(21, 69]$ 
 31. $(\frac{23}{7}, \frac{25}{7})$ 
 33. $[\frac{13}{2}, 16]$ 
 35. $(-\frac{5}{3}, 1]$ 
 37. $(-\infty, -\frac{7}{2}) \cup (\frac{15}{2}, \infty)$

 39. $(-\infty, \frac{1}{2}) \cup (\frac{5}{2}, \infty)$

 41. \emptyset
 43. $(-\infty, 2) \cup (6, \infty)$

 45. \emptyset 47. \emptyset
 49. $[-4, 0]$ 
 51. $(-\infty, \infty)$ 
 53. $(3, 15)$ 
 55. $(-1, 3]$ 
 57. $(-\infty, \infty)$ 
 59. $[-2, 3)$ 

61. $[73, 113]$ for an A,
 $(113, 115)$ for an A+.
 63. $(1140, 1600]$

2.3 Exercises

1. $\{\frac{3}{2}, -1\}$ 3. $\{7\}$
 5. $\{\frac{-3}{2}, -3\}$ 7. $\{-3, 1\}$
 9. $\{2\}$ 11. $\{3, 11\}$

13. $\{0, 6\}$ 15. $\{\frac{3}{8}\}$
 17. $\{17, 19\}$ 19. $\{\frac{1}{2} \pm \sqrt{2}\}$
 21. $\{-5, 9\}$ 23. $\{\frac{6}{5}, 6\}$
 25. $\{-5, -3\}$ 27. $\{-5, \frac{3}{2}\}$
 29. $\{-9, -1\}$ 31. $\{-13, 5\}$
 33. $\{-16, -6\}$ 35. $\{-\frac{4}{3}, 1\}$
 37. $\{0.17 \pm 0.86i\}$
 39. $\{0, \frac{2}{3}\}$ 41. $\{-\frac{17}{7}, 3\}$
 43. Two complex conjugate solutions
 45. Two real solutions
 47. $\{-4.5 \pm 4.5i\}$
 49. $\{-14, -6\}$ 51. $\{2, 14\}$
 53. $\{\frac{-1 \pm \sqrt{7}}{2}\}$ 55. $\{-3, 9\}$
 57. $\{-16, 12\}$ 59. $\{-7, -6\}$
 61. $\{0, 6\}$ 63. $\{-1, 2\}$
 65. $\{1, 2, \frac{3 \pm \sqrt{17}}{2}\}$
 67. $\{\pm 3, \pm \sqrt{7}\}$
 69. 4.5 seconds 71. 4.8 seconds
 75. $(3x - 1 - \sqrt{5})(3x - 1 + \sqrt{5})$
 77. $(5x - 1 - i)(5x - 1 + i)$

2.4 Exercises

1. $\{-3, 4\}$ 3. $\{8, 13\}$
 5. $\{\pm\sqrt{2}, \pm i\sqrt{5}\}$ 7. $\{1 \pm 2i, 1 \pm \sqrt{3}\}$
 9. $\{\frac{1}{8}, 27\}$ 11. $\{\pm 2i, \pm 3\}$
 13. $\{-1, \pm 2, 3\}$ 15. $\{1, -\frac{8}{27}\}$
 17. $\{-1, -2, -3\}$ 19. $\{\pm 1, 3\}$
 21. $\{-\frac{5}{2}, 0, 3\}$ 23. $\{\pm 2, \pm 5i\}$
 25. $\{\pm 2, -\frac{6}{5}\}$ 27. $\{\pm \frac{3}{2}, \pm \frac{3i}{2}\}$
 29. $\{-\frac{5}{2}, 0, \frac{4}{7}\}$

31. $\left\{-\frac{4}{3}, \frac{2 \pm 2i\sqrt{3}}{3}\right\}$
 33. $\left\{-3, \frac{3 \pm 3i\sqrt{3}}{2}\right\}$
 35. $\left\{\frac{5}{2}\right\}$ 37. $\{1\}$
 39. $\{4\}$ 41. $\{0, 2, 3\}$
 43. $\left\{-\frac{1}{5}, \frac{1}{7}\right\}$ 45. $\left\{-1, 0, \frac{2}{5}\right\}$
 47. $\left\{\frac{8}{3}\right\}$ 49. $\left\{-3, -\frac{13}{4}\right\}$
 51. $b = -4, c = -12, \text{ and } d = 0$
 53. $a = 1, c = -36, \text{ and } d = -144$
 55. $a = 15, b = -16, \text{ and } c = -5$

2.5 Exercises

1. $\left\{-\frac{3}{2}\right\}$ 3. $\{3 \pm \sqrt{10}\}$
 5. $\{-3 \pm \sqrt{6}\}$ 7. $\{-2\}$
 9. \emptyset
 11. $(-\infty, -3) \cup (-3, 3) \cup (3, \infty)$
 13. $\left\{\frac{5}{2}, \frac{7}{2}\right\}$
 15. $\{1, -\sqrt{5}, 2 + \sqrt{5}\}$
 17. $\frac{35}{12}$ hours, or 2 hours and 55 minutes
 19. 7.5 hours
 21. 20 weeks
 23. 45 minutes





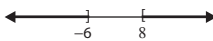

2.6 Exercises

1. $\{0\}$ 3. \emptyset 5. $\{1\}$
 7. $\left\{\frac{2}{3}\right\}$ 9. \emptyset 11. $\left\{\frac{29}{8}\right\}$
 13. $\{6\}$ 15. \emptyset 17. $\{-2, 1\}$
 19. $\{1\}$ 21. $\{10\}$
 23. $\{4\}$ 25. $\{2\}$
 27. $\{-32\}$ 29. $\left\{\pm \frac{125}{343}\right\}$
 31. $\{-2, 5\}$ 33. $\{7, 10\}$
 35. $a = \pm \sqrt{c^2 - b^2}$
 37. $m = \frac{k}{\omega^2}$ 39. $v = \pm \sqrt{\frac{Fr}{m}}$
 41. $h = \pm \sqrt{\frac{w}{23}}$
 43. $c = \pm \sqrt{\frac{2gm}{r}}$
 45. $b = \pm \sqrt{c^2 - a^2}$
 47. $a = \sqrt[3]{\frac{uP^2}{4\pi^2}}$

Chapter 2 Project

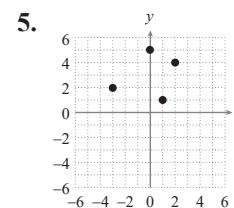
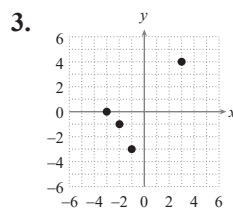
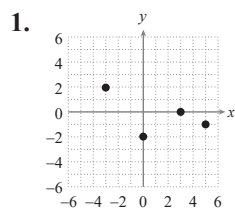
1. Scenario 1: \$472.97
 Scenario 2: \$550.32
 Scenario 3: \$450.77
 Scenario 4: \$458.19
 Scenario 5: \$802.54
 3. Scenario 1: \$4402.56
 Scenario 2: \$1311.52
 Scenario 3: \$3136.96
 Scenario 4: \$3893.12
 Scenario 5: \$760.96

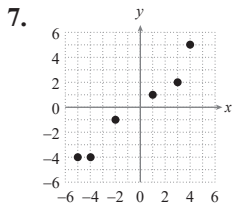
Chapter 2 Review Exercises

1. \emptyset (Contradiction)
 3. $x = 6.25$ 5. $x = 3, 4$
 7. $z = -\frac{10}{7}, 0$ 9. $x = -3, 4$
 11. $c = \frac{2A}{h} - b$
 13. $C = \frac{5}{9}(F - 32)$
 15. \$85
 17. $(4, \infty)$ 
 19. $(1, \infty)$ 
 21. $[-7, 4)$ 
 23. $(-5, -1)$ 
 25. $(-\infty, -6] \cup [8, \infty)$

 27. $(-\infty, 4] \cup [10, \infty)$

 29. $\left\{-\frac{2}{5}, 3\right\}$ 31. $\{2 \pm 3i\}$
 33. $\{4 \pm \sqrt{2}\}$ 35. $\{3 \pm i\sqrt{7}\}$
 37. $\left\{-4, \frac{5}{2}\right\}$ 39. $\left\{\frac{19 \pm \sqrt{701}}{17}\right\}$
 41. $\{\pm 1, \pm \sqrt{2}\}$ 43. $\{-6, 4\}$
 45. $\{\pm \sqrt{2}, 4\}$ 47. $\{1, \pm 2i\}$
 49. $\{-1, 0, 4\}$ 51. $\left\{\frac{3}{2}, 2\right\}$
 53. $b = -2$ and $c = -8$
 55. -5 57. $\{0, 3\}$
 59. $\{-5\}$ 61. $\{-4\}$
 63. $\{2\}$ 65. $\left\{-\frac{3}{2}, 5\right\}$
 67. $\{3\}$ 69. $r = \sqrt{\frac{3V}{\pi h}}$

Chapter 3: Equations and Inequalities in Two Variables

3.1 Exercises





9. III 11. IV

13. Positive x -axis

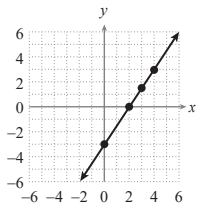
15. III 17. IV

19. II 21. IV

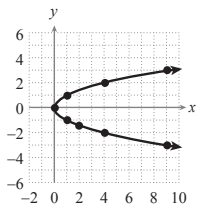
23. I

25. Negative y -axis

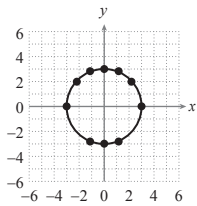
27. $\left\{ (0, -3), (2, 0), \left(3, \frac{3}{2}\right), (4, 3) \right\}$



29. $\left\{ (0, 0), (1, \pm 1), (4, \pm 2), (9, \pm 3), (2, -\sqrt{2}) \right\}$



31. $\left\{ (0, \pm 3), (\pm 3, 0), (-1, \pm 2\sqrt{2}), (1, \pm 2\sqrt{2}), (\pm\sqrt{5}, 2) \right\}$



33. $\sqrt{34}, \left(\frac{-7}{2}, \frac{1}{2}\right)$

35. $\sqrt{58}, \left(\frac{3}{2}, \frac{7}{2}\right)$

37. $2\sqrt{2}, (-1, -1)$

39. $4\sqrt{34}, (3, -8)$

41. $10, (1, -6)$

43. $3\sqrt{13}, \left(2, \frac{1}{2}\right)$

45. $10\sqrt{2}, (3, 3)$

47. $x = 2$ or 18

49. $x = 10, y = 1$

51. 12

53. $2\sqrt{29} + \sqrt{26} + 5\sqrt{2}$

55. 54

57. 1.25 kilometers

59. a. 249.19 meters

b. $\left(\frac{133}{2}, \frac{709}{2}\right)$

61. area = $\frac{15}{2}$ 63. area = 25

65. area = 17 67. area = 48

69. $x = [-5, 6]; y = [-8, 9]$

71. $x = [-3, 6]; y = [-4, 5]$

73. $x = [-6, 8]; y = [-9, 7]$

3.2 Exercises

1. $(x+4)^2 + (y+3)^2 = 25$

3. $(x-7)^2 + (y+9)^2 = 9$

5. $x^2 + y^2 = 6$

7. $(x-\sqrt{5})^2 + (y-\sqrt{3})^2 = 16$

9. $(x-7)^2 + (y-2)^2 = 4$

11. $(x+3)^2 + (y-8)^2 = 2$

13. $(x-4)^2 + (y-8)^2 = 10$

15. $x^2 + y^2 = 85$

17. $\left(x + \frac{7}{2}\right)^2 + \left(y - \frac{17}{2}\right)^2 = \frac{53}{2}$

19. $(x+6)^2 + \left(y - \frac{3}{2}\right)^2 = \frac{125}{4}$

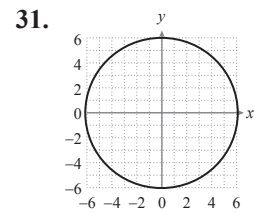
21. $\left(x + \frac{13}{2}\right)^2 + (y+7)^2 = \frac{365}{4}$

23. $(x-4)^2 + (y-3)^2 = 25$

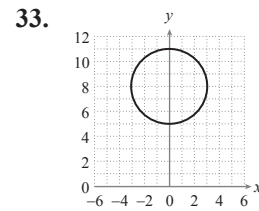
25. $(x-2)^2 + y^2 = 4$

27. $(x-2)^2 + (y-4)^2 = 49$

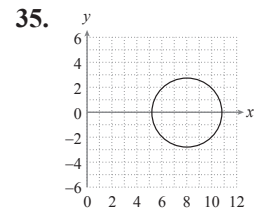
29. $(x+3)^2 + (y+2)^2 = 64$



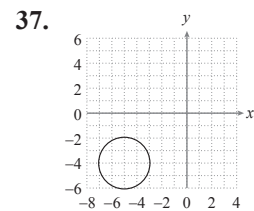
$(0, 0), r = 6$



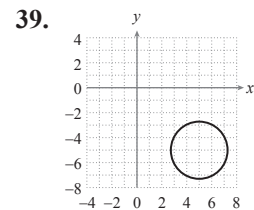
$(0, 8), r = 3$



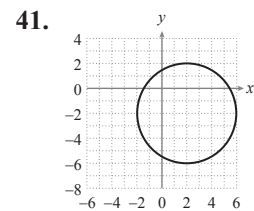
$(8, 0), r = 2\sqrt{2}$



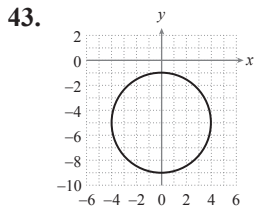
$(-5, -4), r = 2$



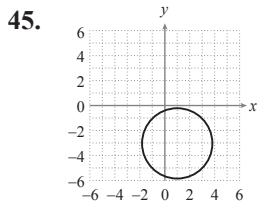
$(5, -5), r = \sqrt{5}$



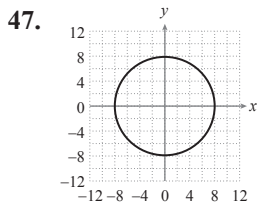
$(2, -2), r = 4$



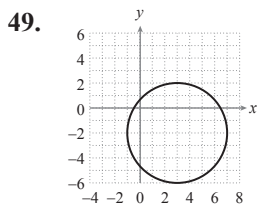
$(0, -5), r = 4$



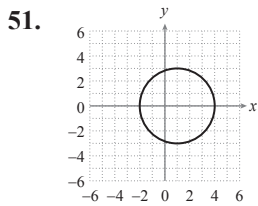
$(1, -3), r = 2\sqrt{2}$



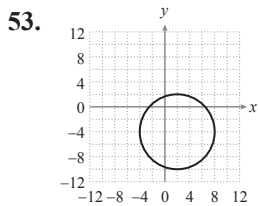
$(0, 0), r = 8$



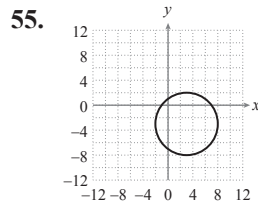
$(3, -2), r = 4$



$(1, 0), r = 3$



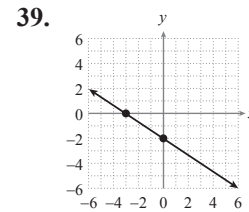
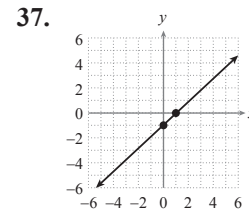
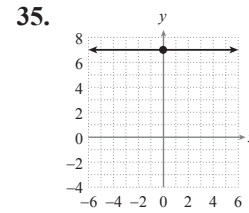
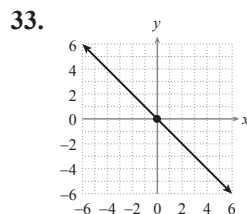
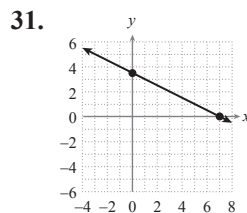
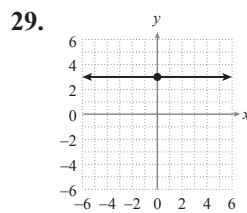
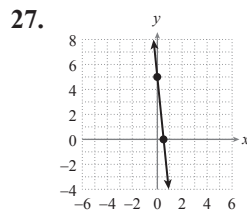
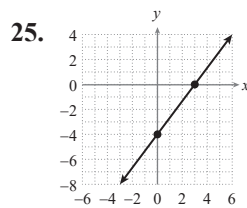
$(2, -4), r = 6$



$(3, -3), r = 5$

3.3 Exercises

1. Yes 3. No 5. No
 7. No 9. Yes 11. Yes
 13. Yes 15. No 17. No
 19. No 21. No 23. Yes

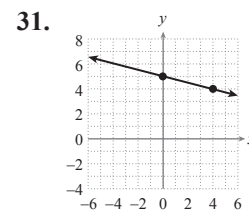
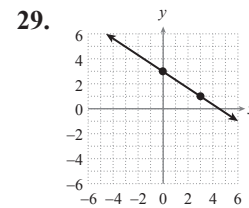


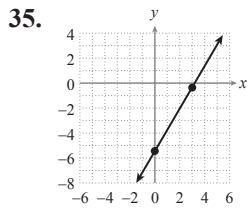
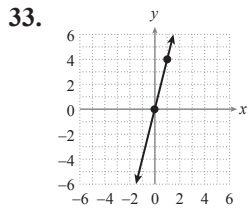
41. e 43. c 45. f

47. $a = P - b - c$
 49. $j = 24,000 + 9b;$
 $b = \frac{j - 24,000}{9}; \text{Yes}$

3.4 Exercises

1. -4 3. 0
 5. Undefined 7. $\frac{2}{3}$
 9. $\frac{1}{6}$ 11. -7
 13. -3 15. $-\frac{9}{13}$
 17. $-\frac{1}{4}$ 19. 0
 21. Undefined 23. 2
 25. $\frac{7}{6}$ 27. $-\frac{5}{2}$





37. $y = \frac{3}{4}x - 3$ 39. $y = -\frac{5}{2}x - 7$

41. $y = -5x - 9$ 43. $3x - 2y = 3$

45. $y = 5$ 47. $10x - y = 31$

49. $3x + y = 26$ 51. $4x + 3y = 5$

53. $x = 2$ 55. $y = -1$

57. $2x + 7y = 52$

59. $y = 5$ 61. $15x - 8y = 0$

63. c 65. e 67. d

69. a. \$2225 b. \$2100 c. \$0.25

71. \$325

3.5 Exercises

1. $y = 4x + 9$ 3. $y = 3x - 11$

5. $y = -9$ 7. $y = x$

9. $y = \frac{7}{6}x + \frac{53}{6}$

11. Yes 13. Yes 15. Yes

17. No 19. No 21. No

23. No 25. No 27. Yes

29. No

31. $y = -\frac{1}{3}x - 1$ 33. $y = 7$

35. $y = -\frac{1}{4}x - \frac{3}{4}$

37. $y = x + 3$ 39. $y = -3x + 28$

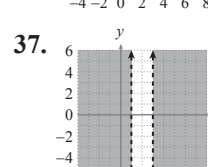
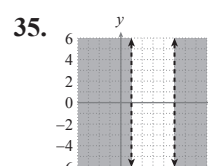
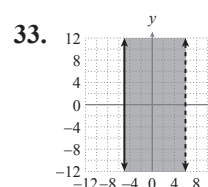
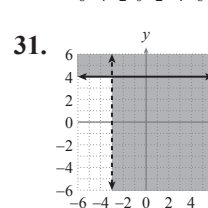
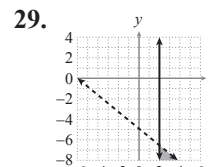
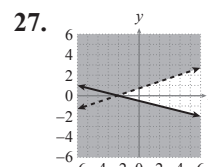
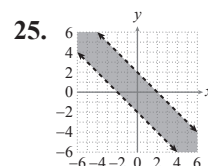
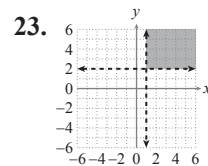
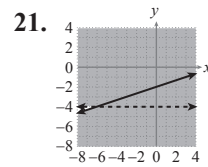
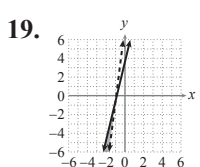
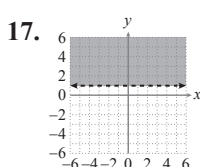
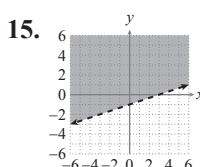
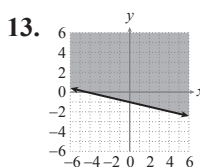
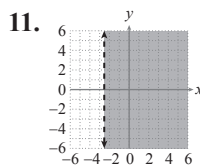
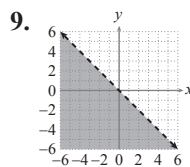
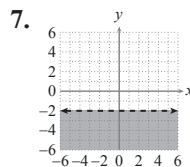
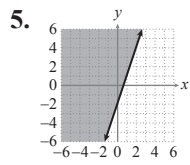
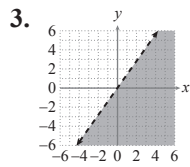
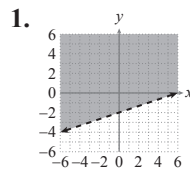
41. No 43. No 45. No

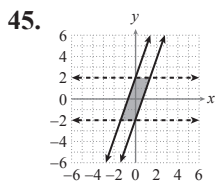
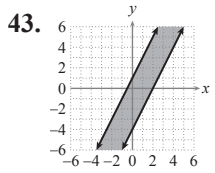
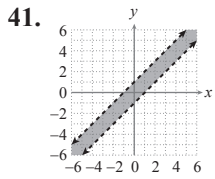
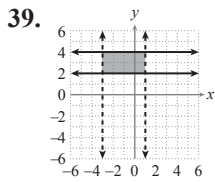
47. No 49. Yes 51. No

53. No 55. No 57. Yes

59. $41\frac{2}{3}$ ft

3.6 Exercises

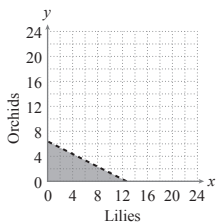




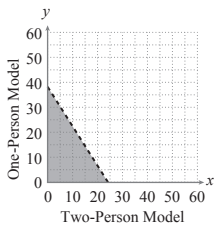
47. h 49. b

51. g 53. c

55. $12x + 22y < 150$



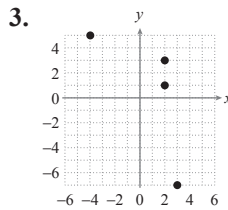
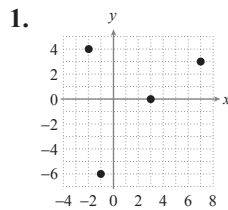
57. $73x + 46y < 1750$



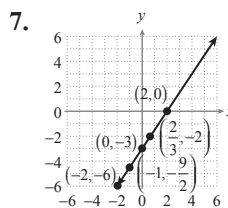
Chapter 3 Project

- Shelbyville Tower: approx. 47.5 ft;
Brockton Tower: 75 ft;
Springfield Tower: approx. 60.6 ft; Ogdenville Tower: approx. 109.5 ft
- No; attachment point: 29.4 ft from the top

Chapter 3 Review Exercises



5. Positive x -axis



$$(2, 0), (0, -3), \left(-1, -\frac{9}{2}\right), \left(\frac{2}{3}, -2\right), (-2, -6)$$

9. a. $\sqrt{2}$ b. $\left(\frac{5}{2}, -\frac{13}{2}\right)$

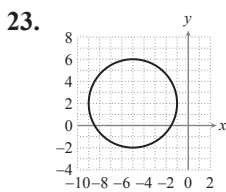
11. a. $2\sqrt{13}$ b. $(-5, 3)$

13. 2 15. 24

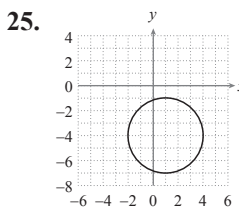
17. $(x - \sqrt{5})^2 + (y + \sqrt{2})^2 = 16$

19. $(x - 2)^2 + (y + 1)^2 = 20$

21. Center: $(-3, 1)$; Radius: $2\sqrt{2}$

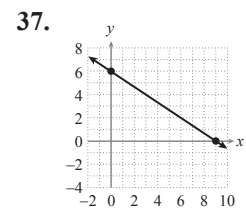
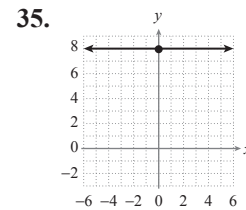
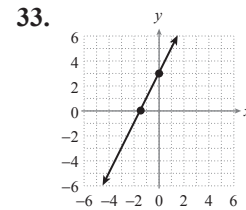


$r = 4; (h, k) = (-5, 2)$



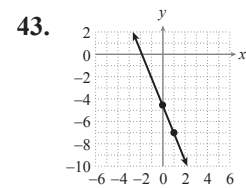
$r = 3; (h, k) = (1, -4)$

27. No 29. Yes 31. No



39. 12

41. Undefined



45. $x - y = 5$

47. $y = \frac{5}{9}x - 2$

49. $9x - 2y = 31$

51. $W = 0.08s + 2800$

53. Perpendicular

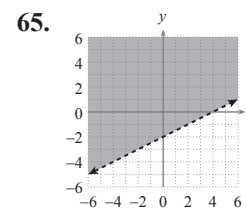
55. $y = 3x + 10$

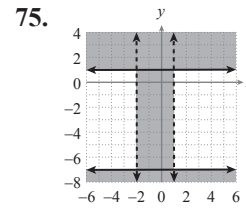
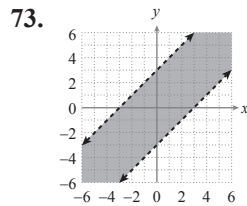
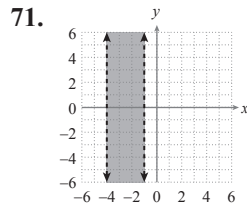
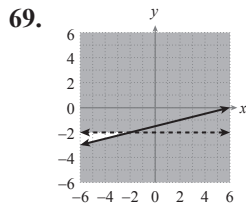
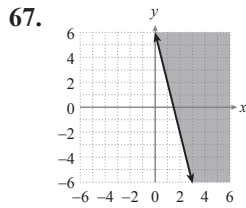
57. $y = 2x - 3$

59. $y = -\frac{4}{3}x + 6$

61. $x = 7$

63. Yes





77. $3x + 4y \geq 1500$

Chapter 4: Relations, Functions, and Their Graphs

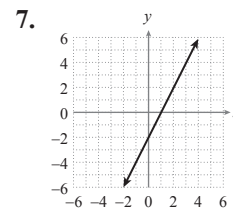
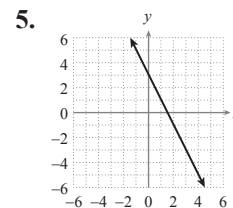
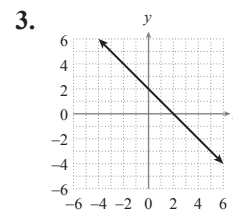
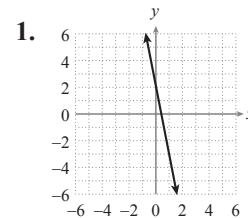
4.1 Exercises

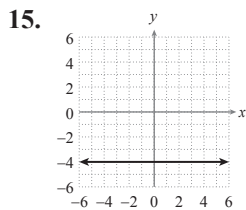
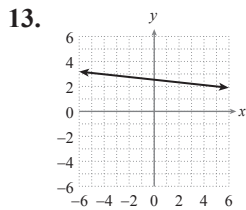
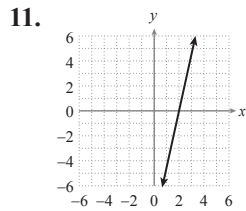
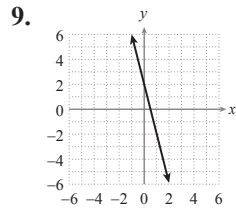
1. Dom = $\{-2\}$, Ran = $\{5, 3, 0, -9\}$
3. Dom = $\{\pi, -2\pi, 3, 1\}$,
Ran = $\{2, 4, 0, 7\}$
5. Dom = \mathbb{Z} , Ran = even integers
7. Dom = \mathbb{Z} ,
Ran = $\{\dots, -2, 1, 4, \dots\}$
9. Dom = Ran = \mathbb{R}
11. Dom = $[0, \infty)$, Ran = \mathbb{R}
13. Dom = \mathbb{R} , Ran = $\{-1\}$
15. Dom = $\{0\}$, Ran = \mathbb{R}
17. Dom = $[-3, 1]$, Ran = $[0, 4]$
19. Dom = $[0, 3]$, Ran = $[1, 5]$
21. Dom = $[-1, 3]$, Ran = $[-4, 3]$
23. Dom = All males with siblings,
Ran = All people who have brothers
25. Not a function;
 $(-2, 5)$ and $(-2, 3)$
27. Function
29. Not a function; $(6, -1)$ and $(6, 4)$
31. Not a function;
 $(-1, 0)$ and $(-1, 4)$
33. Function 35. Function
37. Function
39. Not a function;
 $(-1, -1)$ and $(-1, 1)$
41. Function 43. Function
45. Not a function; $(1, -2)$ and $(1, 2)$

47. $f(x) = -6x^2 + 2x, f(-1) = -8$
49. $f(x) = \frac{-x+10}{3}, f(-1) = \frac{11}{3}$
51. $f(x) = -2x - 10, f(-1) = -8$
53. 1 55. 3
57. $x = -3, 2, 3$
59. a. 10 b. $x^2 + x - 2$
c. $2ax + 3a + a^2$ d. $x^4 + 3x^2$
61. a. 8 b. $3x - 1$
c. $3a$ d. $3x^2 + 2$
63. a. -2 b. $-6x + 16$
c. $-6a$ d. $-6x^2 + 10$
65. a. $i - 3$ b. $\sqrt{2-x} - 3$
c. $\sqrt{1-x-a} - \sqrt{1-x}$
d. $\sqrt{1-x^2} - 3$
67. $2x + h - 5$
69. $\frac{-1}{(x+h+2)(x+2)}$
71. $5(2x+h)$ 73. 2
75. $\frac{\sqrt{x+h} - \sqrt{x}}{h}$
77. Dom = Cod = Ran = \mathbb{R}
79. Dom = Cod = Ran = \mathbb{Z}
81. Dom = Cod = \mathbb{N} ,
Ran = $\{6, 7, 8, \dots\}$
83. $[1, \infty)$
85. $(-\infty, -2) \cup (-2, 3) \cup (3, \infty)$
87. \mathbb{R}

89. $(-\infty, \frac{1}{3}) \cup (\frac{1}{3}, \infty)$
91. $(-\infty, 2) \cup (2, \infty)$
93. $[-6, \infty)$ 95. $(-\infty, 0) \cup (0, \infty)$
97. A function is a special relation in which every element of the domain is paired with exactly one element of the range.

4.2 Exercises



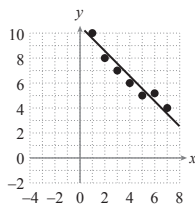


17. b 19. a

21. $f(x) = -x + 3$

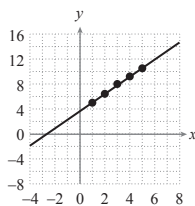
23. $f(x) = 2x - 3$

25. a. $y = -0.93x + 10.14$



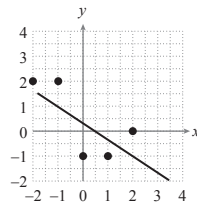
b. $r \approx -0.969$

27. a. $y = 1.36x + 3.82$



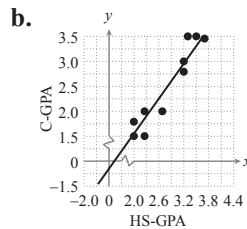
b. $r \approx 0.998$

29. a. $y = -0.7x + 0.4$



b. $r \approx -0.730$

31. a. $y = 1.20x - 0.85$

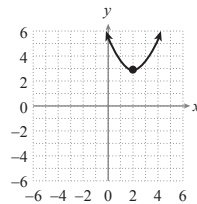


c. $r \approx 0.951$

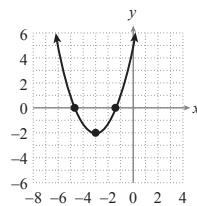
33. Neither. They are equal because the correlation is the absolute value.

4.3 Exercises

1. Vertex: (2,3); no x-int.

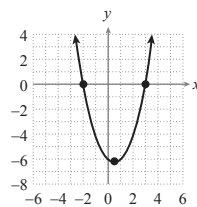


3. Vertex: (-3,-2);
x-int.: $x = -3 \pm \sqrt{2}$

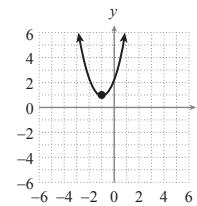


5. Vertex: $(\frac{1}{2}, -\frac{25}{4})$;

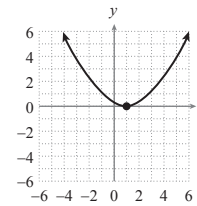
x-int.: $x = -2, 3$



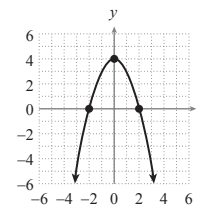
7. Vertex: (-1,1); no x-int.



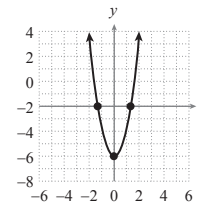
9. Vertex: (1,0); x-int.: $x = 1$



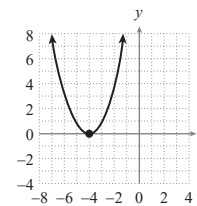
11. Vertex: (0,4); x-int.: $x = -2, 2$



13. Vertex: (0,-6); x-int.: $x = \pm \frac{\sqrt{6}}{2}$



15. Vertex: (-4,0); x-int.: $x = -4$



17. b 19. d

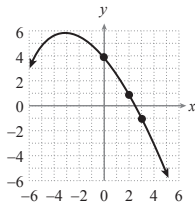
21. a. $f(x) = -\frac{1}{2}(x+2)(x-1)$

b. $(-\frac{1}{2}, \frac{9}{8})$

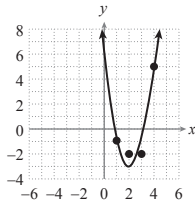
23. a. $f(x) = 3(x+1)(x-3)$

b. (1,-12)

25. $f(x) = -0.167x^2 - 1.17x + 4$



27. $f(x) = 2x^2 - 8.2x + 5.5$



29. a. $f(x) = x^2 - 2x + 2$

b. (1,1)

31. a. $f(x) = -x^2 + 2x - 3$

b. (1,-2)

33. 5 and 5 35. (2,1)

37. The dimensions should be 5 inches by 10 inches by 10 feet

39. 49 people; \$2401

41. 12 and 24 43. 375 units

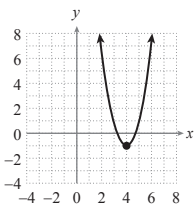
45. 25 sets of golf clubs

47. 112 feet 49. 164 feet

51. $h(t) = -15.88t^2 + 60.17t + 7$; the maximum height of the baseball was approximately 64 feet.

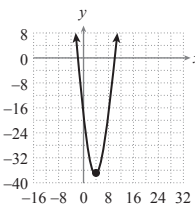
53. Vertex: (4,-1);

$$x\text{-int.: } x = \frac{8 \pm \sqrt{2}}{2}$$

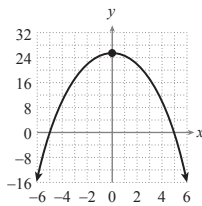


55. Vertex: (4,-36);

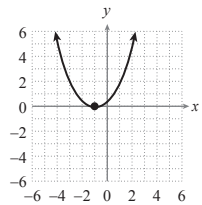
$$x\text{-int.: } x = -2, 10$$



57. Vertex: (0,25); x-int.: $x = -5, 5$

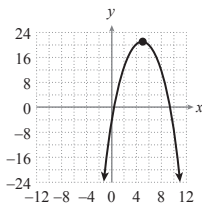


59. Vertex: (-1,0); x-int.: $x = -1$

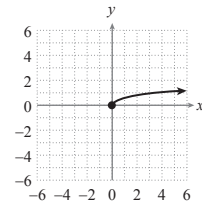


61. Vertex: (5,21);

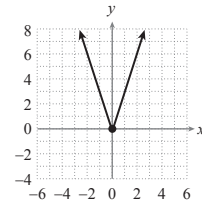
$$x\text{-int.: } x = 5 \pm \sqrt{21}$$



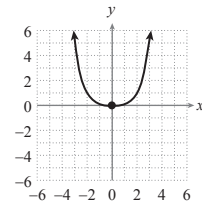
9.



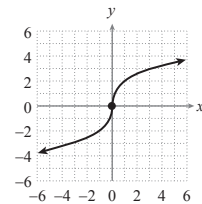
11.



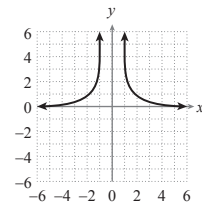
13.



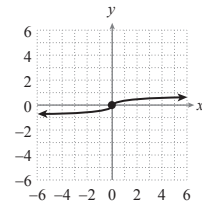
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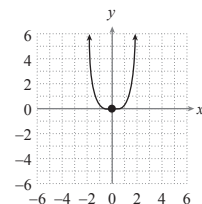
17.



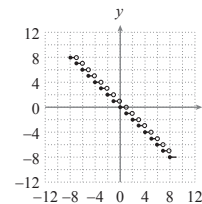
19.



21.

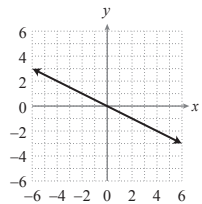


23.

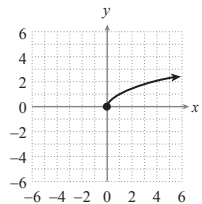


4.4 Exercises

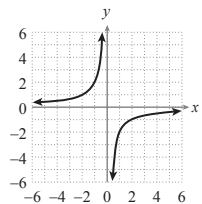
1.



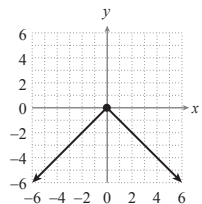
3.

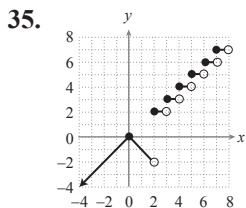
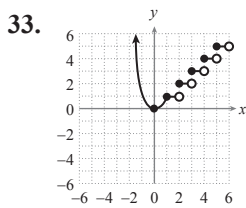
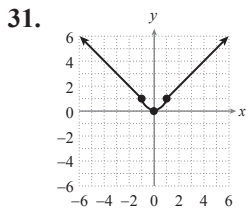
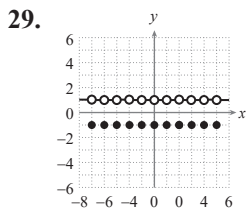
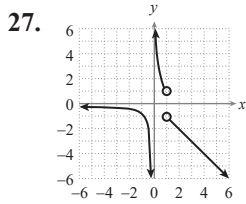
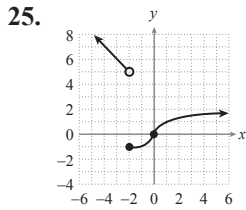


5.



7.





37. j 39. a 41. i

43. e 45. f

4.5 Exercises

1. $A = kbh$ 3. $W = \frac{k}{d^2}$
 5. $r = \frac{k}{t}$ 7. $x = ky^3z^2$
 9. $y = 18\sqrt{5}$ 11. $y = 60\sqrt{2}$
 13. $y = 0.75$ 15. $y = 0.0024$

17. $z = 112$ 19. $z = 48$
 21. $a = 10\sqrt{3}$ 23. $a = 36$
 25. $a = 108$ 27. 256 feet
 29. 20.60 31. 6.7 meters
 33. 1.25 centimeters

35. 34.54 inches 37. 164.7872 in.²
 39. 9 watts 41. \$43
 43. 17.28 ohms 45. 19.66 inches
 47. 210 cubic inches
 49. $P(\sigma, \varepsilon) = \frac{\sigma^2}{2\varepsilon}$

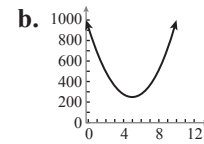
4.6 Exercises

1. a. If x represents the side length of each square cut from a corner,
 $V(x) = (60 - 2x)(20 - 2x)x$
 $= 4x^3 - 160x^2 + 1200x$
 for $0 \leq x \leq 10$.
 b. Yes; for example,
 $V(4) = 2496 \text{ cm}^3$.
 c. Approximately 2525 cm^3 ,
 obtained by letting
 $x = 4.5 \text{ cm}$.
 d. A height of 5 cm will lead to a width of 10 cm and consequently a length of 50 cm, so the ratio of length to width will be 5:1.

3. a. $V(t) = P\left(1 - \frac{2t}{9}\right)$ for $0 \leq t \leq 3$
 b. $\frac{9}{4}$ years, or 2 years and 3 months
 c. $V(1) = \frac{7}{9}P$

5. a. $d = \sqrt{(1 + m^2)x^2 + 2bmx + b^2}$
 b. $d = \sqrt{x^2 + b^2}$
 c. $d = \sqrt{(1 + m^2)}|x|$
 d. $d = 2|x|$

7. a. $s(x) = 30x^2 - 300x + 1000$ for $0 \leq x \leq 10$



- c. 1000, 250
 9. a. 9.25×10^6
 b. 1.45 times, or 145%
 c. They aren't weightless, but instead in free fall. Astronauts fall toward Earth at the same rate as the craft they're in, making it appear as though they're floating.

11. a. $A = 6V^{\frac{2}{3}}$

b. $A = 600 \text{ mm}^2$

13. a. $C = 8x + 4y = 8x + \frac{7200}{x}$,
 where x is the length of fence along the boundary

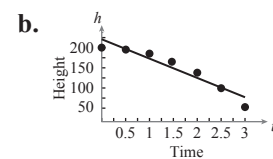
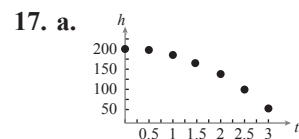
b. 30 ft

15. a. $R(x) = x(30 - 3x)$,
 $C(x) = 36 + 6x$,

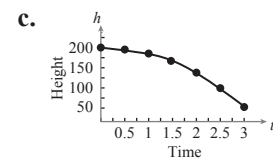
$P(x) = -3x^2 + 24x - 36$

b. 2 c. 4

- d. \$18 for \$12 maximum profit



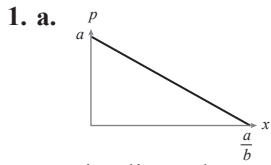
$h(t) = -48t + 220$;
 approximately 4.58 s; 220 ft



$h(t) = -16t^2 + 200$;
 approximately 3.54 s; 200 ft

- d. The quadratic model is more accurate.

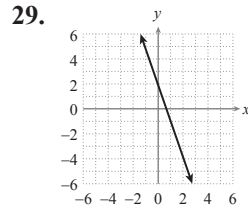
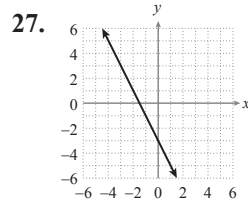
Chapter 4 Project



- b. p is a linear decreasing function of x .
- c. $x = 0$ corresponds to $p = a$, so a price of a corresponds to no sales.
- d. $p = 0$ corresponds to $x = \frac{a}{b}$, which is the maximum feasible sales figure.
- e. $R(x) = xp = x(a - bx)$
 $= -bx^2 + ax$
- f. R is a quadratic function.
- g. The graph of R is a downward-opening parabola.

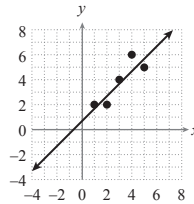
Chapter 4 Review Exercises

- 1. Dom = $\{-2, -3\}$,
Ran = $\{-9, -3, 2, 9\}$; No
- 3. Dom = \mathbb{R} , Ran = $\{2\}$; Yes
- 5. Dom = \mathbb{R} , Ran = \mathbb{R} ; Yes
- 7. Dom = $[0, \infty)$, Ran = $[4, \infty)$; Yes
- 9. Dom = $\{-2, 4\}$,
Ran = $\{-1, 5\}$; Yes
- 11. $f(x) = 3\sqrt{x+11} - 4$;
 $f(-2) = 5$
- 13. 4
- 15. $x = -1, x = 3$
- 17. $\sqrt{x+h}$
- 19. $\sqrt[3]{(x+h)^2}$
- 21. Dom = \mathbb{N} , Cod = \mathbb{R} ,
Ran = $\left\{\frac{3}{4}, \frac{3}{2}, \frac{9}{4}, \dots\right\}$
- 23. \mathbb{R}
- 25.

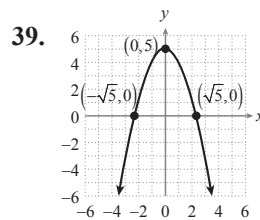
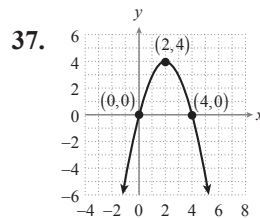
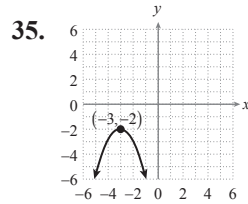


31. $f(x) = 2x - 1$

33. a. $y = x + 0.8$

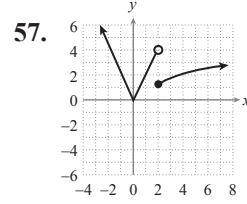
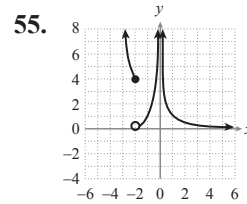
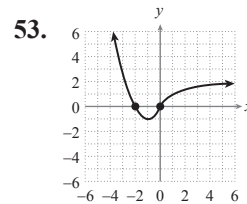
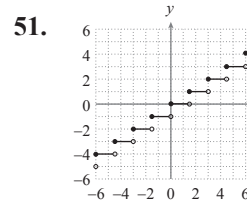
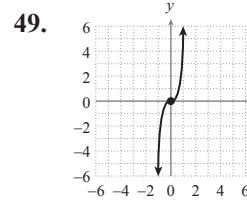
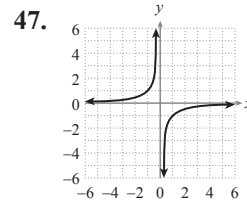
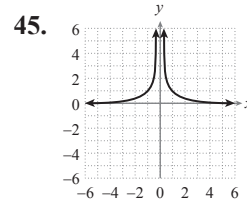
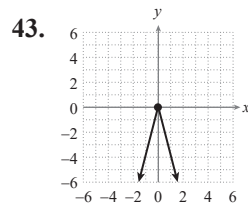


b. $r \approx 0.884$



41. a. $f(x) = x^2 - 3x + 1$

b. $(1.5, -1.25)$



59. $y = \frac{ka^3}{\sqrt{b}}$

61. $y = 72$

63. 7.44×10^7 m

65. a. $C(x) = \frac{12,000}{x} + 13x$, where x is the length of fence along the road.

b. Approximately 30.38 ft (along the road) by 39.50 ft (not along the road); approximately \$789.94

Chapter 5: Working with Functions

5.1 Exercises

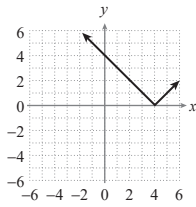
1. $f(x) = x^2$ 3. $f(x) = \sqrt[3]{x}$

5. $f(x) = \sqrt{x}$ 7. $f(x) = \frac{1}{x^2}$

9. $f(x) = x^3$ 11. $f(x) = |x|$

13. $f(x) = \sqrt{x}$ 15. $f(x) = x^3$

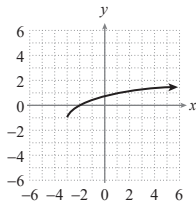
17.



Dom = \mathbb{R} ,

Ran = $[0, \infty)$

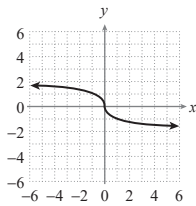
19.



Dom = $[-3, \infty)$,

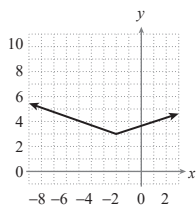
Ran = $[-1, \infty)$

21.



Dom = Ran = \mathbb{R}

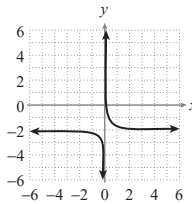
23.



Dom = \mathbb{R} ,

Ran = $[3, \infty)$

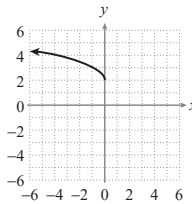
25.



Dom = $(-\infty, 0) \cup (0, \infty)$,

Ran = $(-\infty, -2) \cup (-2, \infty)$

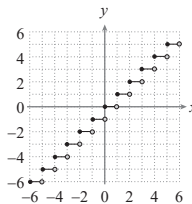
27.



Dom = $(-\infty, 0]$,

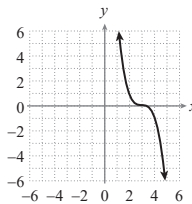
Ran = $[2, \infty)$

29.



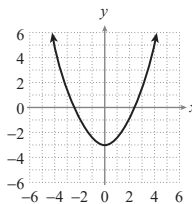
Dom = \mathbb{R} , Ran = \mathbb{Z}

31.



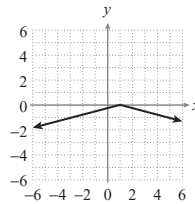
Dom = Ran = \mathbb{R}

33.



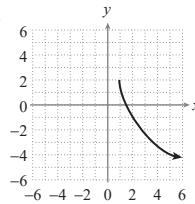
Dom = \mathbb{R} , Ran = $[-3, \infty)$

35.



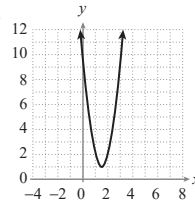
Dom = \mathbb{R} , Ran = $(-\infty, 0]$

37.



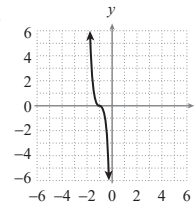
Dom = $[1, \infty)$, Ran = $(-\infty, 2]$

39.



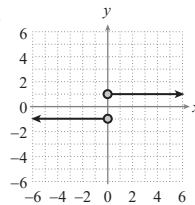
Dom = \mathbb{R} , Ran = $[1, \infty)$

41.



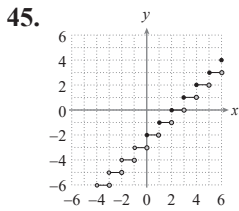
Dom = \mathbb{R} , Ran = \mathbb{R}

43.



Dom = $(-\infty, 0) \cup (0, \infty)$,

Ran = $\{-1, 1\}$



Dom = \mathbb{R} , Ran = \mathbb{Z}

47. $f(x) = (x-4)^2 + 2$

49. $f(x) = (-x-2)^2 = (x+2)^2$

51. $f(x) = (-x+1)^3$

53. $f(x) = -\sqrt{x+5}$

55. $f(x) = \sqrt{-\frac{x}{2}} + 3$

57. $f(x) = -|x-8|-2$

59. $f(x) = -\sqrt{-(x+1)}$

61. $f(x) = \sqrt{2x}$

63. $f(x) = -\sqrt{x+4}$

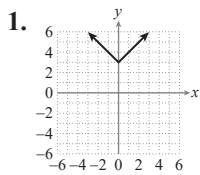
65. $f(x) = 1 - (x-3)^3$

73. $f(x) = |x+4|-1$

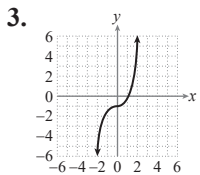
75. $f(x) = -\sqrt{6-x} + 2$

77. $f(x) = 6 - (x-3)^2$

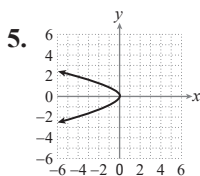
5.2 Exercises



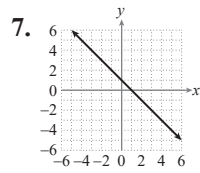
Even function; y-axis symmetry



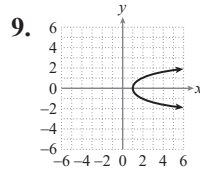
Neither; no symmetry



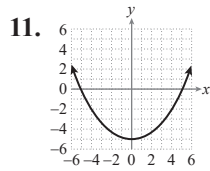
Not a function; x-axis symmetry



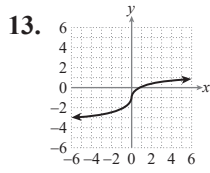
None of the above



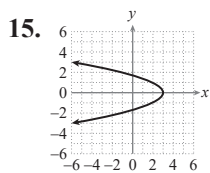
Not a function; x-axis symmetry



Even function; y-axis symmetry



None of the above



Not a function; x-axis symmetry

17. Inc. on $(-\infty, 2)$,

Dec. on $(2, \infty)$

19. Inc. on $(-\infty, -3)$,

Dec. on $(-3, \infty)$

21. Constant on \mathbb{R}

23. Dec. on $(-\infty, 4)$,

Inc. on $(4, \infty)$

25. Dec. on $(-\infty, -3)$,

Inc. on $(-3, -1)$,

Constant on $(-1, \infty)$

27. a. local min at -1 , local max at 2

b. value at -1 is 0 , value at 2 is 3

29. a. local min at -1 , local max at 2

b. value at -1 is -12 ,
value at 2 is 15

31. a. local min at -2 ,
local max at 0 , local min at 3

b. value at -2 is $\frac{5}{3}$, value at 0 is 7 , value at 3 is $-\frac{35}{4}$

33. a. local min at 5

b. value at 5 is 2

35. a. local max at -2

b. value at -2 is 1

37. a. local min at 3

b. value at 3 is -2

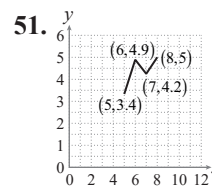
39. 11 41. 2

43. $\frac{2-\sqrt{2}}{2}$

45. $2c+h$ 47. $-\frac{1}{12}$

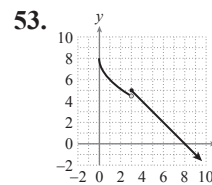
49. a. $[a,b]$ b. $[b,c], [b,d]$

c. $[a,c], [a,d], [c,d]$



Inc. on $(5, 6)$ and $(7, 8)$

Dec. on $(6, 7)$



Dec. on $(0, 3) \cup (3, \infty)$

55. The average rate of change is m for any interval.

57. $2cp + hp + q$; The difference quotient approaches $2cp + q$ as h gets very small.

59. Nothing; Exercise 49a illustrates this conclusion.

5.3 Exercises

1. a. 2 b. -8 c. -15 d. $-\frac{3}{5}$

3. a. -3 b. -1 c. 2 d. 2

5. a. 12 b. 18 c. -45 d. -5

7. a. 3 b. 1 c. 2 d. 2

9. a. 6 b. 0 c. 9 d. 1

11. a. 5 b. -1 c. 6 d. $\frac{2}{3}$

13. a. 3 b. 5 c. -4 d. -4

15. a. $|x| + \sqrt{x}$, Dom = $[0, \infty)$

b. $\frac{|x|}{\sqrt{x}}$, Dom = $(0, \infty)$

17. a. $x^2 + x - 2$, Dom = \mathbb{R}

b. $\frac{1}{x+1}$,
Dom = $(-\infty, -1) \cup (-1, 1) \cup (1, \infty)$

19. a. $x^3 + 3x - 8$, Dom = \mathbb{R}

b. $\frac{3x}{x^3 - 8}$,
Dom = $(-\infty, 2) \cup (2, \infty)$

21. a. $-2x^2 + |x + 4|$, Dom = \mathbb{R}

b. $\frac{-2x^2}{|x + 4|}$,
Dom = $(-\infty, -4) \cup (-4, \infty)$

23. 2 25. 0 27. 8

29. 3 31. 1 33. $\frac{1}{3}$

35. a. $\frac{4-2x}{3x}$,
Dom = $(-\infty, 0) \cup (0, \infty)$

b. $\frac{3}{4x-2}$,
Dom = $(-\infty, \frac{1}{2}) \cup (\frac{1}{2}, \infty)$

37. a. $|x^3 - 2|$, Dom = \mathbb{R}

b. $|x - 3|^3 + 1$, Dom = \mathbb{R}

39. a. $\sqrt{\frac{x-1}{2}}$, Dom = $[1, \infty)$

b. $\frac{\sqrt{x-1} + 1}{2}$, Dom = $[1, \infty)$

41. a. $-3x^2 - 4$, Dom = \mathbb{R}

b. $9x^2 - 12x + 6$, Dom = \mathbb{R}

43. a. $\sqrt{x^2 - 1}$,
Dom = $(-\infty, -1] \cup [1, \infty)$

b. $x - 1$, Dom = \mathbb{R}

45. $g(x) = \frac{2}{x}$, $h(x) = 5x - 1$,
 $f(x) = g(h(x))$

47. $g(x) = x + \sqrt{x} - 5$,
 $h(x) = x + 2$, $f(x) = g(h(x))$

49. $g(x) = \frac{\sqrt{x}}{x^2}$, $h(x) = x - 3$,
 $f(x) = g(h(x))$

51. $g(x) = x - 3$, $h(x) = |x^2 + 3x|$,
 $f(x) = g(h(x))$

53. $g(x) = \sqrt{x+5}$

55. $g(x) = -x^3 - 7$

57. $V = 3\pi r^3$

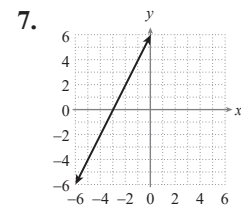
59. $V = \frac{1}{12}\pi r^2 t^2$

61. $(f \circ g)(x) = \sqrt[3]{\frac{-x^3}{3x^2 - 9}}$,

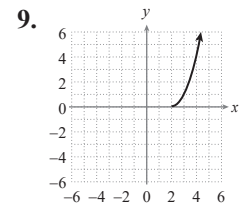
$(f \circ g)(-x) = \sqrt[3]{\frac{x^3}{3x^2 - 9}}$
 $= -(f \circ g)(x)$

63. Yes 65. Yes 67. No

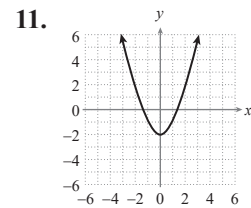
69. No 71. No



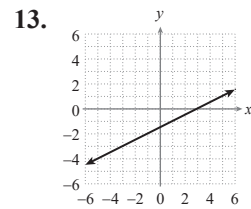
Dom = \mathbb{R} , Ran = \mathbb{R}



Dom = $[2, \infty)$, Ran = $[0, \infty)$



Dom = \mathbb{R} , Ran = $[-2, \infty)$



Dom = \mathbb{R} , Ran = \mathbb{R}

15. Not a one-to-one function

$f(-1) = f(1) = 1$

17. Restrict to $[0, \infty)$

19. Inverse exists

21. Inverse exists

23. Inverse exists

25. Restrict to $[2, \infty)$

27. Restrict to $[12, \infty)$

29. $f^{-1}(x) = (x + 2)^3$

31. $r^{-1}(x) = \frac{-2x - 1}{3x - 1}$

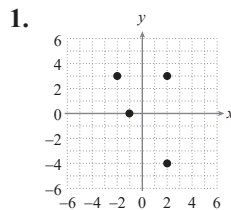
33. $F^{-1}(x) = (x - 2)^{\frac{1}{3}} + 5$

35. $V^{-1}(x) = 2x - 5$

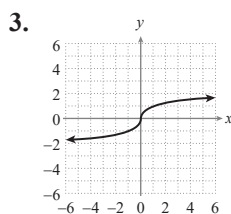
37. $h^{-1}(x) = (x + 2)^{\frac{5}{3}}$

39. $J^{-1}(x) = \frac{x - 2}{3x}$

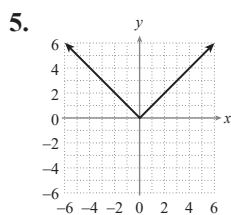
5.4 Exercises



Dom = $\{2, -1, -2\}$,
Ran = $\{-4, 3, 0\}$



Dom = Ran = \mathbb{R}



Dom = \mathbb{R} , Ran = $[0, \infty)$

41. $h^{-1}(x) = (x-6)^{\frac{1}{7}}$

43. $r^{-1}(x) = \frac{x^5}{2}$ 45. $f^{-1}(x) = \frac{x^3}{54}$

47. $f^{-1}(x) = \sqrt{x-2} + 3$
or $f^{-1}(x) = -\sqrt{x-2} + 3$

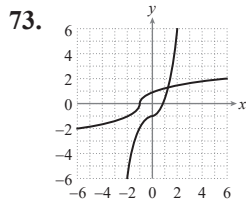
49. $f^{-1}(x) = \sqrt[4]{x+2} - 1$
or $f^{-1}(x) = -\sqrt[4]{x+2} - 1$

61. f 63. c 65. d

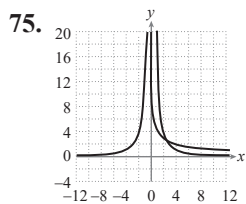
67. 184 72 96 96 72 160 144 8
72 112 160 120 32 8 200

69. REMEMBER
YOUR
SUNBLOCK

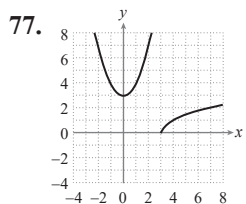
71. BEACH FUN IN THE SUN



Dom = $(-\infty, \infty)$, Ran = $(-\infty, \infty)$



Dom = $(0, \infty)$, Ran = $(0, \infty)$



Dom = $[3, \infty)$, Ran = $[0, \infty)$

Chapter 5 Project

1. $A(r) = \pi r^2$

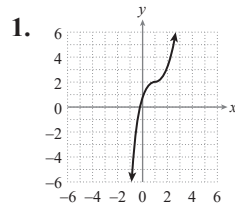
3. $A(t) = 6.76\pi t^2$

5. $r(5.5) = 14.3$ km

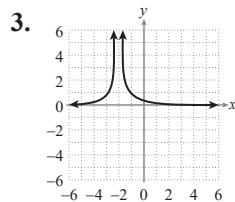
7. $A(5.5) \approx 642.4$ km²

9. Approximately 286.7 km²/hr

Chapter 5 Review Exercises

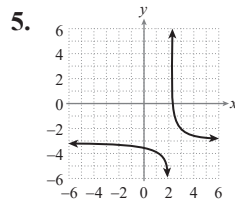


Dom = Ran = \mathbb{R}



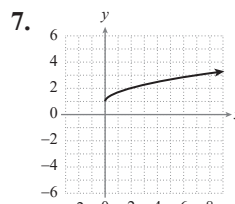
Dom = $(-\infty, -2) \cup (-2, \infty)$,

Ran = $(0, \infty)$



Dom = $(-\infty, 2) \cup (2, \infty)$,

Ran = $(-\infty, -3) \cup (-3, \infty)$



Dom = $[0, \infty)$, Ran = $[1, \infty)$

9. $f(x) = (x-1)^2 - 2$

11. $f(x) = -\sqrt{x} + 4$

13. Even function;
y-axis symmetry

15. Dec. on $(-\infty, 2)$,

Inc. on $(2, \infty)$

17. a. Local min at 1,
local max at 2, local min at 3

b. Value at 1 is 1,
value at 2 is 4, value at 3 is 1

19. $-\frac{1}{3}$ 21. -2

23. a. 3 b. 5 c. -4 d. -4

25. a. -2 b. 18 c. -80 d. $-\frac{4}{5}$

27. a. $\frac{1}{x-2} + \sqrt[3]{x}$,

Dom = $(-\infty, 2) \cup (2, \infty)$

b. $\frac{1}{\sqrt[3]{x(x-2)}}$,

Dom =
 $(-\infty, 0) \cup (0, 2) \cup (2, \infty)$

29. a. $x^2 + \sqrt[3]{x} - 5$, Dom = \mathbb{R}

b. $\frac{x^2 - 4}{\sqrt[3]{x-1}}$,

Dom = $(-\infty, 1) \cup (1, \infty)$

31. $-\frac{9}{2}$ 33. $-\frac{2}{3}$

35. a. $\frac{1}{\sqrt{x-2}}$, Dom = $(2, \infty)$

b. $\frac{1}{\sqrt{x-4}} + 2$, Dom = $(4, \infty)$

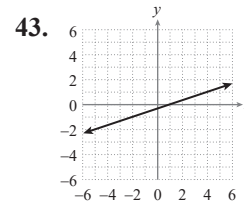
37. a. $3\sqrt{x-3}$, Dom = $[3, \infty)$

b. $\sqrt{3x-3}$, Dom = $[1, \infty)$

39. $g(x) = \frac{\sqrt{x}}{x^2}$, $h(x) = x + 2$,

$f(x) = g(h(x))$

41. $g(x) = \frac{2}{x} + 1$



Dom = Ran = \mathbb{R}

45. $r^{-1}(x) = \frac{x+2}{7x}$

47. $f^{-1}(x) = (x+6)^5$

49. $f^{-1}(x) = \frac{-x-3}{x-2}$

51. $f^{-1}(x) = \frac{x-3}{8}$

Chapter 6: Polynomial and Rational Functions

6.1 Exercises

19. Yes 21. Yes 23. Yes

25. $1 \pm 2i$ 27. $-3, \frac{1}{2}$

29. $\pm\sqrt{3}, \pm\sqrt{5}$ 31. $-\frac{5}{2}$

33. $0, 4 \pm 3i$ 35. $\pm 1, \pm 2i\sqrt{2}$

37. 7th-degree; lead coef. = 4;

$$j(x) \rightarrow -\infty \text{ as } x \rightarrow -\infty$$

$$j(x) \rightarrow \infty \text{ as } x \rightarrow \infty$$

39. 5th-degree; lead coef. = -6;

$$h(x) \rightarrow \infty \text{ as } x \rightarrow -\infty$$

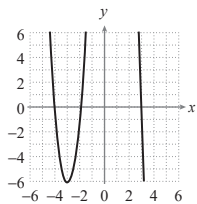
$$h(x) \rightarrow -\infty \text{ as } x \rightarrow \infty$$

41. 4th-degree; lead coef. = -2;

$$f(x) \rightarrow -\infty \text{ as}$$

$$x \rightarrow -\infty \text{ and } x \rightarrow \infty$$

43.



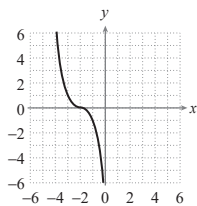
$$g(x) \rightarrow \infty \text{ as } x \rightarrow -\infty;$$

$$g(x) \rightarrow -\infty \text{ as } x \rightarrow \infty$$

$$x\text{-int: } (-4, 0), (-2, 0), (3, 0);$$

$$y\text{-int: } (0, 24)$$

45.

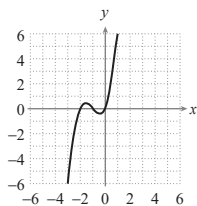


$$h(x) \rightarrow \infty \text{ as } x \rightarrow -\infty;$$

$$h(x) \rightarrow -\infty \text{ as } x \rightarrow \infty$$

$$x\text{-int: } (-2, 0), (0, 0)$$

47.



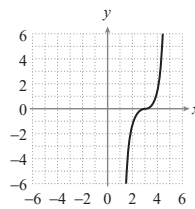
$$s(x) \rightarrow -\infty \text{ as } x \rightarrow -\infty;$$

$$s(x) \rightarrow \infty \text{ as } x \rightarrow \infty$$

$$x\text{-int: } (-2, 0), (-1, 0), (0, 0);$$

$$y\text{-int: } (0, 0)$$

49.



$$g(x) \rightarrow -\infty \text{ as } x \rightarrow -\infty;$$

$$g(x) \rightarrow \infty \text{ as } x \rightarrow \infty$$

$$x\text{-int: } (3, 0); y\text{-int: } (0, -243)$$

51. $p(x) = \left(\frac{1}{2}\right)(x+2)$

$$\times(x+1)(x-1)(x-3)$$

53. $p(x) = -(x-1)(x-2)(x-3)$

55. e 57. a 59. f

61. d 63. f 65. b

67. $(-\infty, -2) \cup (3, \infty)$

69. $(-\infty, -2) \cup (-1, 0)$

71. $[-2, 1] \cup [3, \infty)$

73. $[-5, -1] \cup [1, 4]$

75. $\left(-\frac{1}{2}, 2\right)$

77. $(-\infty, -4) \cup (2, 3)$

79. All integers between 5 and 27, inclusive

81. All integers between 11 and 23, inclusive

83. Between 3490 and 17,740 phones, inclusive.

85. About 141.4 weeks

6.2 Exercises

1. $3x^2 - x + 1 + \frac{5x-1}{2x^2+2}$

3. $x - 2 + \frac{-2}{x^2 - 4x + 4}$

5. $4x^2 - 14x + 29 + \frac{-65}{x+2}$

7. $x^3 + 6x^2 - 2x + 5 + \frac{2x+5}{3x^2-1}$

9. $2x^3 - 3x^2 + 2x - 5$

11. $x^3 + 3x^2 + 10x + 10 + \frac{22}{x-3}$

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13. $3x^2 + 5x + 9 + \frac{45}{3x-5}$

15. $2x - 5 + \frac{7}{x+3}$

17. $x^2 - ix + 6 + \frac{1+i}{2x-i}$

19. $x^2 + 3$ 21. $p(1) = 4$

23. c is a zero 25. c is a zero

27. $p(1) = 12$ 29. c is a zero

31. c is a zero 33. c is a zero

35. c is a zero 37. $p(5) = -2$

39. c is a zero

41. $x^2 - 4x + 2 + \frac{-1}{x+5}$

43. $x^7 - 3x^2 + \frac{3}{x+1}$

45. $4x^2 - 4x + 2$

47. $x^4 - x^3 - x^2 - 7x - 14 - \frac{10}{x-2}$

49. $x^3 - x^2 + x$

51. $2x^2 - 4ix + 17 + \frac{8+48i}{x-3i}$

53. $f(x) = -x^2 - x + 12$

55. $f(x) = -x^2 + 4x - 13$

57. $f(x) = x^4 - 12x^3 + 54x^2 - 108x + 81$

59. $f(x) = 3x^4 + 9x^3 - 9x^2 - 21x + 18$

61. $SA = (x+5)(x+2) = x^2 + 7x + 10$

6.3 Exercises

1. $\pm\left\{\frac{1}{3}, \frac{2}{3}, 1, \frac{4}{3}, 2, \frac{8}{3}, 4, 8\right\}, \left\{-4, \frac{1}{3}, 2\right\}$

3. $\pm\{1, 2, 3, 4, 6, 8, 12, 24\}, \{\pm 2i, 2, 3\}$

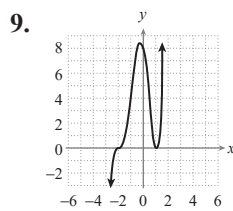
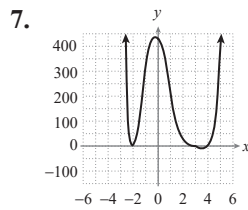
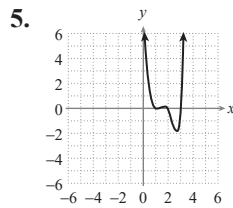
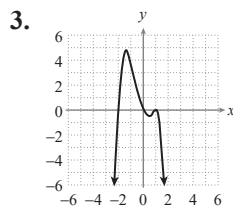
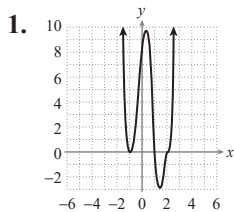
5. $\pm\{1, 2, 7, 14\}, \{1, 2, 7\}$

7. $\pm\left\{\frac{1}{2}, 1, \frac{3}{2}, \frac{5}{2}, 3, 5, \frac{15}{2}, 15\right\}, \left\{-1, \frac{5}{2}, 3\right\}$

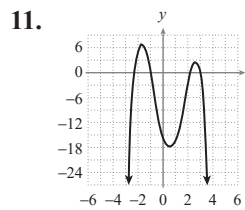
9. $\pm\left\{\frac{1}{3}, 1, 3\right\}, \{-1, 1, -i, i\}$

11. $\pm\{1, 11\}, \{-11, -1, 1\}$
 13. $\{-1, 1, -i, i\}$
 15. $\{-1, 2 - 3i, 2 + 3i\}$
 17. $\{-2i, 2i, 2, 3\}$
 19. $\{4, 1 - 2i, 1 + 2i\}$
 21. $\{-5i, 5i, -2, 1\}$
 23. $\{-11, -1, 1\}$
 25. 0 pos., 3 or 1 neg.
 27. 2 or 0 pos., 1 neg.
 29. 3 or 1 pos., 1 neg.
 31. 1 pos., 1 neg.
 33. 3 or 1 pos., 0 neg.
 35. 0 pos., 0 neg.
 37. $[-5, 1]$ 39. $[-1, 6]$
 41. $[-3, 6]$ 43. $[-3, 3]$
 45. $[-3, 6]$ 47. $\{-4, -1, 1\}$
 49. $\{-1, 2, 5\}$ 51. $\{2, 3, \pm 2\sqrt{2}\}$
 53. $\pm\{\sqrt{5}, i\sqrt{5}\}$ 55. $\left\{-2, -\frac{1}{2}, 6\right\}$
 57. $f(-3) = -84, f(-1) = 16$
 59. $f(2) = -15, f(3) = 24$
 61. $f(2) = 15, f(3) = -24$
 63. $\{-1, 2, 5\}$ 65. $\left\{-\frac{7}{3}, \pm 1\right\}$
 67. $\left\{-1, -\frac{2}{5}, 2, \frac{7}{3}\right\}$
 69. $\left\{\pm 3, -2, -\frac{1}{3}\right\}$ 71. $\left\{-5, \pm 1, \frac{5}{2}, 4\right\}$
 73. $\{-3, -2, -1\}$ 75. $\{-9, \pm\sqrt{2}\}$
 77. $\left\{-3, -\frac{1}{2}, 8\right\}$ 79. $\left\{\pm 2, -\frac{3}{4}, 1\right\}$
 81. $\left\{\sqrt[3]{-2}, \pm\frac{\sqrt{6}}{2}, \frac{5}{3}\right\}$

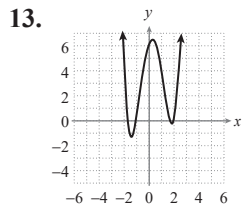
6.4 Exercises



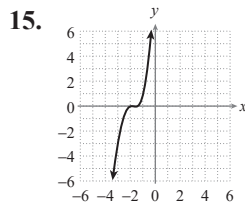
$f(x) = (x+2)^3(x-1)^2$



$s(x) = -(x-3)(x+1) \times (x-\sqrt{5})(x+\sqrt{5})$



$H(x) = (x-2)(x+1) \times (x-\sqrt{3})(x+\sqrt{3})$



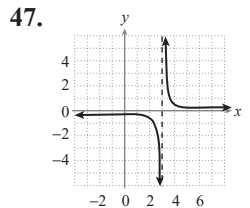
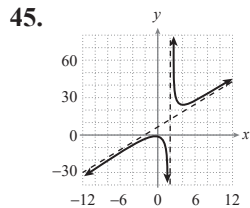
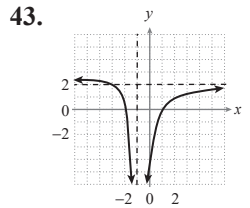
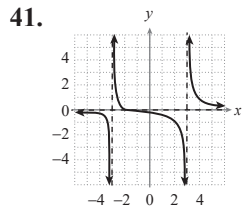
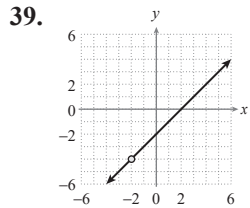
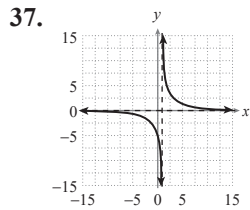
$f(x) = (x+2)^2(2x+3)$

17. $\{-2, 1\}$ 19. $\{-2, 1, \pm i\sqrt{5}\}$
 21. $\{-3, 1, \pm 2i\}$ 23. $\{\pm 1, \pm 4i\}$
 25. $(x-3+2i)(x-3-2i) \times (x-4)(x+1)$
 27. $(x-1-3i)(x-2)(x+1)$
 29. $(x+\sqrt{7})(x-\sqrt{7})(x-2+3i) \times (x-2-3i)$
 31. $(x-2)(x+1)(x-1+2i) \times (x-1-2i)$
 33. $x(x-3)(x-1)(x+11)$
 35. $(x-2)(x-2+4i)(x-2-4i)$
 37. $f(x) = -2x^3 + 18x^2 - 32x - 52$
 39. $f(x) = 2x^5 + 2x^4 - 10x^3 - 2x^2 + 16x - 8$
 41. $f(x) = 3x^4 - 18x^3 + 12x^2 - 72x$
 43. $f(x) = -x^3 + 2x^2 + 14x - 40$
 45. $f(x) = -x^3 + 4x^2 + 15x - 68$
 47. a. $V(x) = 4x(5-x)(9-x)$
 b. $x = 0, x = 5, x = 9$
 c. $x = 0$ and $x = 5$
 49. a. $V(x) = x(17-2x)(9-2x)$
 b. $x = 0, x = \frac{9}{2}, x = \frac{17}{2}$
 c. $x = 0$ and $x = \frac{9}{2}$

6.5 Exercises

1. $x = 1$
 3. No vertical asymptote
 5. $x = 2$ 7. $x = 0$
 9. $x = -\frac{1}{2}$
 11. No vertical asymptote
 13. $x = 7$ 15. $x = -2$
 17. $x = -2, x = 2$ 19. $y = 0$
 21. No horizontal or oblique asymptote
 23. $y = 0$ 25. $y = 2$
 27. $y = 3x + 6$ 29. $y = 0$
 31. $y = 0$ 33. $y = x - 11$

35. $y = 5x + 4$



49. a. $x = -2$ b. $y = 0$
c. None d. None e. $(0, 5)$

51. a. $x = 9$ b. $y = 0$
c. None d. None

e. $\left(0, -\frac{1}{3}\right)$

53. a. $x = -1, x = 1$ b. None

c. $y = x$ d. $(\sqrt[3]{3}, 0)$

e. $(0, 3)$

55. a. $x = 1$ b. None c. $y = 3x$
d. None e. $(0, -3)$

57. $(-\infty, -2) \cup (-1, 1)$

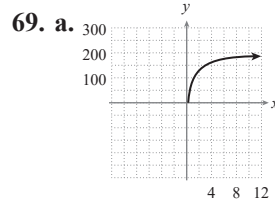
59. $(-8, -2) \cup (2, \infty)$

61. $(-\infty, -2) \cup (-2, 3)$

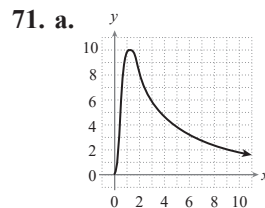
63. $(0, 3)$

65. $(-2, -1) \cup (1, \infty)$

67. $(-\infty, -1) \cup \left[-\frac{1}{2}, 0\right)$



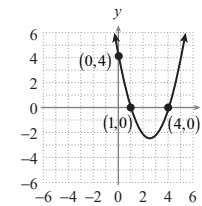
b. April's fish population approaches a maximum of 200 fish.



b. The concentration of the drug disappears in the long run.

13. x-int: 1, 4; y-int: 4

$g(x) \rightarrow \infty$ as $x \rightarrow \pm \infty$



15. $\left[\frac{5}{2}, 3\right]$

17. $[-2, -1] \cup [1, 4]$

19. $(-\infty, 0) \cup (0, 1) \cup (2, \infty)$

21. All integers between 4 and 30, inclusive

23. $11x + 35 + \frac{100}{x-3}$

25. $2x^3 + 2x^2 - 2x - 3 + \frac{-2x-2}{x^2-x}$

27. $p(1) = 90$ 29. $p\left(\frac{2}{3}\right) = -\frac{7}{3}$

31. $-x^3 + 2x^2 - 7x + 23$

33. $-x^3 + 7x^2 + x - 3 + \frac{-1}{x-1}$

35. $f(x) = x^2 - 4x - 12$

37. $f(x) = 2(x^2 - 4)(x - 3)$

39. $\pm\left\{\frac{1}{2}, 1, \frac{3}{2}, 3, \frac{9}{2}, 9\right\}, \left\{1, \frac{3}{2}, 3\right\}$

41. $\pm\{1, 3, 9\}, \{-3, -1\}$

43. $\left\{1, \frac{3}{2}, 3\right\}$ 45. $\{-3, -1\}$

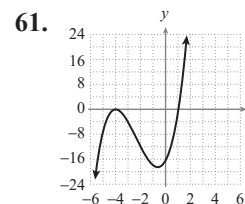
47. 4, 2 or 0 pos., 2 or 0 neg.

49. $[-3, 7]$ 51. $\left\{-\frac{5}{2}, -\frac{1}{2}, 7\right\}$

53. $f(2) = 3; f(4) = -15$

55. $\{\pm 3i, 4\}$ 57. $\{3, 2 \pm \sqrt{3}\}$

59. $\left\{-\frac{1}{2}, 2\right\}$



Chapter 6 Project

1. $P(x) = -3x^2 + 5500x - 729,000$

3. \$4933 for $x = 1689$
to \$9568 for $x = 144$

5. $[212, 1621]$

Chapter 6 Review Exercises

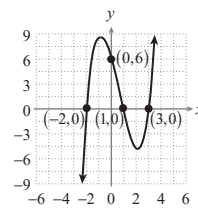
5. $\pm\sqrt{2}, \pm\sqrt{5}$ 7. $\pm\sqrt{2}$

9. $0, \frac{-1 \pm \sqrt{5}}{2}$

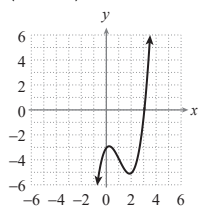
11. x-int: -2, 1, 3; y-int: 6

$f(x) \rightarrow -\infty$ as $x \rightarrow -\infty$;

$f(x) \rightarrow \infty$ as $x \rightarrow \infty$



63. $(x^2 + 1)(x - 3)$



65. $\left\{-1, \frac{5}{3}, \pm 2i\right\}$

67. $\{\pm 2i, -3, \pm 1\}$

69. $(x - 5i)(x + 5i)(x - 6)(x + 1)$

71. $(x + 3)\left(x - \frac{1 + i\sqrt{19}}{4}\right)$

$\times \left(x - \frac{1 - i\sqrt{19}}{4}\right)$

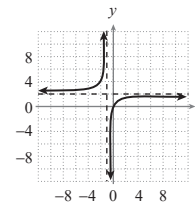
73. $f(x) = x^5 + 3x^4 - 3x^3 - 17x^2 - 18x - 6$

75. $x = \frac{5}{2}$ 77. $x = 0$

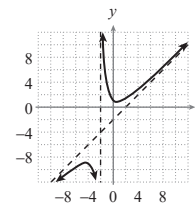
79. $y = 2x + 9$

81. No horizontal or oblique asymptote

83.



85.



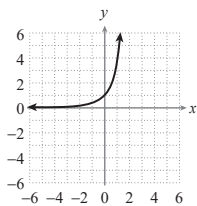
87. $\left(-3, \frac{7}{2}\right]$

89. $\left(-3, \frac{8}{9}\right) \cup (2, \infty)$

Chapter 7: Exponential and Logarithmic Functions

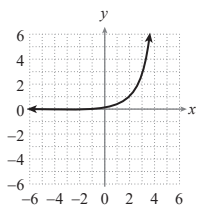
7.1 Exercises

1.



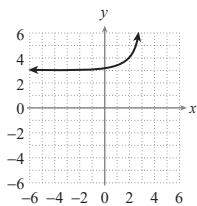
Dom = $(-\infty, \infty)$, Ran = $(0, \infty)$

3.



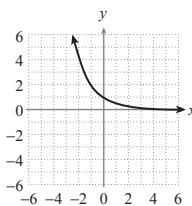
Dom = $(-\infty, \infty)$, Ran = $(0, \infty)$

5.



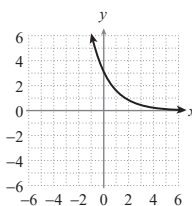
Dom = $(-\infty, \infty)$, Ran = $(3, \infty)$

7.



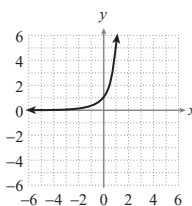
Dom = $(-\infty, \infty)$, Ran = $(0, \infty)$

9.



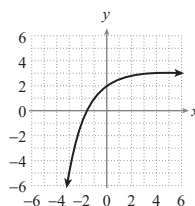
Dom = $(-\infty, \infty)$, Ran = $(0, \infty)$

11.



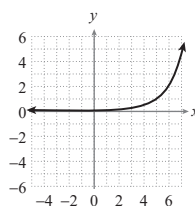
Dom = $(-\infty, \infty)$, Ran = $(0, \infty)$

13.



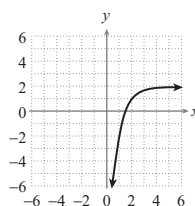
Dom = $(-\infty, \infty)$, Ran = $(-\infty, 3)$

15.

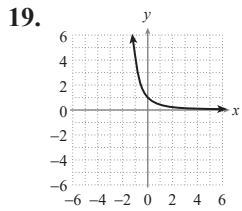


Dom = $(-\infty, \infty)$, Ran = $(0, \infty)$

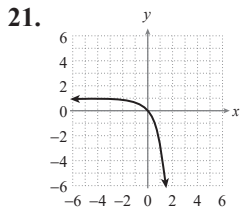
17.



Dom = $(-\infty, \infty)$, Ran = $(-\infty, 2)$



Dom = $(-\infty, \infty)$, Ran = $(0, \infty)$



Dom = $(-\infty, \infty)$, Ran = $(-\infty, 1)$

23. $\{2\}$ 25. $\{-2\}$ 27. $\{-13\}$

29. $\{3\}$ 31. $\{-2\}$

33. $\{-2, -1\}$

35. $\{7\}$ 37. $\{3\}$ 39. $\{9\}$

41. $\{-3\}$ 43. $\{2\}$ 45. $\{-1\}$

47. a 49. i 51. d

53. e 55. h

7.2 Exercises

1. $V \approx 178$ people

3. $C \approx \$8526.20$

5. $W \approx 93$ computers

7. a. $a \approx 0.999567$

b. $A \approx 0.958$ grams

c. $A \approx 0.648$ grams

9. a. 3 years b. 9 years

11. 1118 rabbits

13. The bank offering 2.75% and monthly compounding.

15. Approximately 3.18%

17. \$134,392

19. a. 10 b. 7490 people

c. The function approaches 10,000 as time goes on.

21. a. $a \approx 0.965936$

b. $A \approx 0.707$ kg

c. $A \approx 7.628$ mg

23. a. \$1521.74 b. \$271.74

25. \$9459.48; \$9942.41

27. \$2835.71

29. \$20,000

31. \$7318.71

33. a. \$7647.95 b. \$7647.57

c. Yes; daily compounding is a frequency close enough to continuous compounding to make little difference at the hundredths place.

35. a. Linear:

$$y = 1.06098 \times 10^6 x$$

$$-1.94223 \times 10^9$$

Quadratic:

$$y = 8501.22x^2 - 3.08186 \times 10^7 x$$

$$+ 2.79424 \times 10^{10}$$

Exponential:

$$y = 2.172414 \times 10^{-12} (1.023986)^x$$

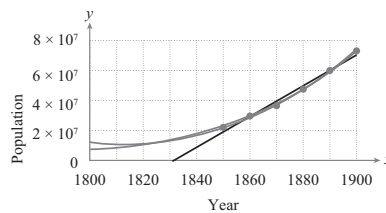
b. Linear: -32,466,000

Quadratic: 12,872,800

Exponential: 7,348,129

Actual: 5,308,483

None of these regression models appear to be very accurate this far from known data, though the population estimates given by the exponential model are closer to the actual population.



7.3 Exercises

1. $4 = \log_5 625$ 3. $3 = \log_x 27$

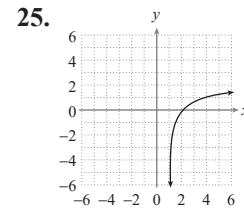
5. $3 = \log_{4.2} C$ 7. $x = \log_4 31$

9. $\sqrt{3} = \log_{4x} 13$ 11. $e^x = \log_2 11$

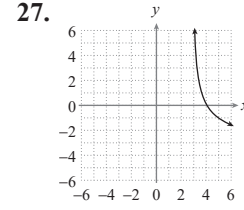
13. $81 = 3^4$ 15. $4 = b^{\frac{1}{2}}$

17. $15 = 2^b$ 19. $W = 5^{12}$

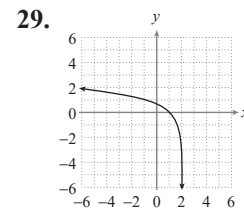
21. $2x = \pi^4$ 23. $e^x = 2$



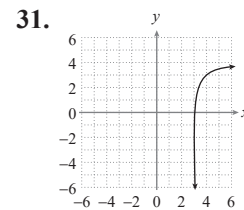
Dom: $(1, \infty)$, Ran: $(-\infty, \infty)$



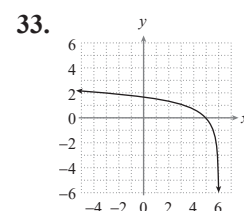
Dom: $(3, \infty)$, Ran: $(-\infty, \infty)$



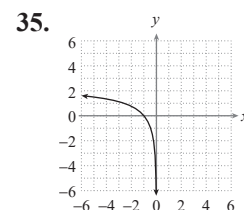
Dom: $(-\infty, 2)$, Ran: $(-\infty, \infty)$



Dom: $(3, \infty)$, Ran: $(-\infty, \infty)$



Dom: $(-\infty, 6)$, Ran: $(-\infty, \infty)$



Dom: $(-\infty, 0)$, Ran: $(-\infty, \infty)$

37. e 39. b 41. h

43. d 45. i 47. -2

49. 3 51. $-\frac{1}{2}$ 53. $\frac{3}{4}$

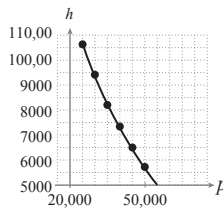
55. 2.89 57. $\frac{5}{3}$ 59. 1
 61. $\frac{1}{5}$ 63. 2 65. {64}
 67. {9} 69. $\left\{-\frac{1}{2}\right\}$ 71. $\left\{\frac{1}{21}\right\}$
 73. {10} 75. {36}
 77. $\left\{\pm\frac{1}{10}\right\}$ 79. {0.18}
 81. $\{\pm\sqrt{e}\}$ or $\{\pm 1.65\}$
 83. {12.89}
 85. {10,000,000,002}

7.4 Exercises

1. $3 + 3\log_5 x$
 3. $2 + \ln p - 3\ln q$
 5. $1 + \log_9 x - 3\log_9 y$
 7. $\frac{3}{2}\ln x + \ln p + 5\ln q - 7$
 9. $\log(2 + 3\log x)$
 11. $1 - \frac{1}{2}\log(x + y)$
 13. $\log_2(y^2 + z) - 4\log_2 x - 4$
 15. $2\log_b x + \frac{1}{2}\log_b y - \log_b z$
 17. $2 + \log_b a + b\log_b c$
 19. $\log\frac{x}{y}$
 21. $\log_5(x + 5)$
 23. $\log_2\left(x^{\frac{4}{3}} + 3x^{\frac{1}{3}}\right)$
 25. $\ln\left(\frac{3p}{q^2}\right)$ 27. $\log\left(\frac{x-10}{x}\right)$
 29. $\ln\left(\frac{z^2}{x^3y^3}\right)$ 31. $\log_5 4$
 33. $\ln 45$ 35. $\log_3 1 = 0$
 37. $\ln 12$ 39. $\log 11$
 41. $\log_8(x^2 - y)$ 43. x^2
 45. $\frac{e^2 p}{x}$ 47. $\frac{x^3}{y^4}$ 49. x^2
 51. 4 53. $12x^2$ 55. 2.04

57. 0.95 59. 0.95 61. 2.45
 63. 3.30 65. 0.74 67. 1.20
 69. 1.86 71. -1 73. 3.85
 75. 0.77 77. -1.76 79. 2
 81. 7 83. 1
 85. $4\sqrt{2} \approx 5.66$ 87. 9.05
 89. 2.08 91. 12
 93. 1,048,576 95. 10.25
 97. 5,011,872 times stronger
 99. 133 decibels
 101. 7.62; yes
 103. a. 15.05 minutes
 b. 7:00 p.m.
 c. 112 °F; no

105. $h(p) = 81,751.7 - 7027.82 \ln p$



7.5 Exercises

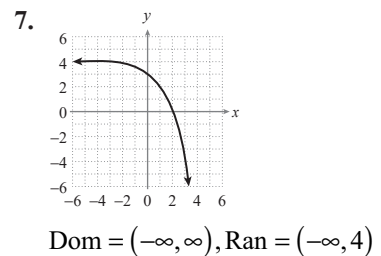
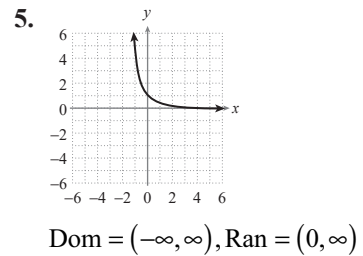
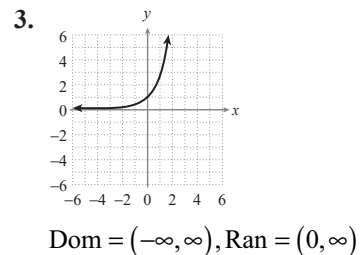
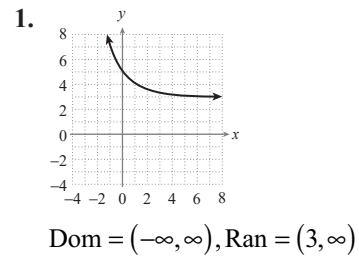
1. $x \approx 0.26$ 3. $x \approx 3.12$
 5. $x \approx 3.89$ 7. $x \approx -2.28$
 9. $x \approx 8.09$ 11. $x \approx 2.68$
 13. $x \approx -1.12$ 15. $x \approx 52.77$
 17. $x \approx \pm 0.71$ 19. $x = -12$
 21. $x \approx 1.32$ 23. $x \approx 3.27$
 25. $x = 125$ 27. $x = 5$
 29. $x \approx 40.17$ 31. $x = 35$
 33. $x \approx 9.38$ 35. $x = 4$
 37. $x = \frac{1}{162}$ 39. $x = 1$
 41. $x \approx 100.04$ 43. No solution
 45. $x = 5$ 47. $x = 8$
 49. $x = \frac{37}{8}$ 51. $x = 5$
 53. No solution 55. $x = 6$
 57. $x = \sqrt{2} - 1$ 59. $x = 2, 3$

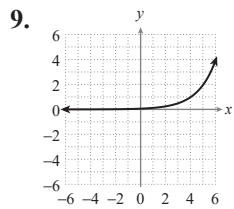
61. $x = 1, 2$ 63. $f(x) = \log 2x^2$
 65. $f(x) = \ln 9x^2$
 67. $f(x) = 256x$
 69. $f(x) = \ln 1 = 0$
 71. $f(x) = \ln 5^x$ 73. $f(x) = \ln 5$
 75. a. 17.36 years
 b. 9.90 years
 77. 4.98 hours 79. 4.99 years
 81. 0.271 years (about 99 days)

Chapter 7 Project

1. 242 3. 20,219

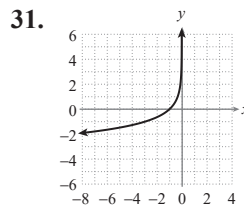
Chapter 7 Review Exercises



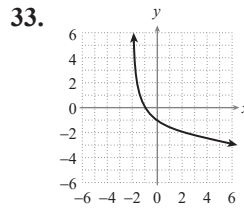


Dom = $(-\infty, \infty)$, Ran = $(0, \infty)$

11. $x = 5$ 13. $x = 2$
 15. $x = -1$ 17. $x = \frac{8}{5}$
 19. $x = 2$ 21. 8 days
 23. a. 173 flies b. 20 flies
 25. $x = \log_3 8$ 27. $\log_4 4096 = 3a$
 29. $3^{-3} = \frac{1}{27}$



Dom = $(-\infty, 0)$, Ran = $(-\infty, \infty)$



Dom = $(-2, \infty)$, Ran = $(-\infty, \infty)$

35. -2 37. -3 39. $\frac{2}{3}$
 41. $x = 27$ 43. $x = \frac{17}{2}$
 45. $x \approx 155.41$
 47. $\frac{3}{2} \log x - \frac{5}{2} \log \pi - \log 2$

49. $3 + 3 \log_3 a$ 51. $\log_2 \left(\frac{a^{\frac{5}{3}}}{b^{\frac{1}{3}} c} \right)$
 53. $\log_2 (x-3)$ 55. $\log_3 \frac{x^2 - 2x}{x^2 + 4}$
 57. $\frac{x}{y^2}$ 59. 6.18 61. 0
 63. a. 251,188,643
 b. 7,079,458
 c. 1,258,925,412
 65. $\frac{6}{\log 321} \approx 2.39$
 67. $\frac{\ln 5}{4 - 3 \ln 5} \approx -1.94$
 69. $\frac{\log 12}{\log 18} \approx 0.86$
 71. -2 73. 73.5
 75. $f(x) = \ln x^3$ 77. $f(x) = \log x^{10}$
 79. $f(x) = \log 7$
 81. 20.4 months (1.7 years)

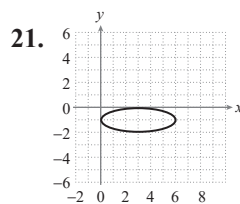
Chapter 8: Conic Sections

8.1 Exercises

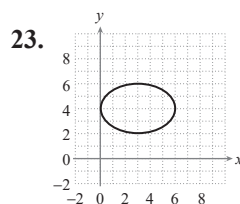
1. Center: $(5, 2)$
 Foci: $(5, 2 \pm \sqrt{21})$
 Vertices: $(5, 7), (5, -3)$
 3. Center: $(-2, -5)$
 Foci: $(-2 \pm \sqrt{6}, -5)$
 Vertices: $(1, -5), (-5, -5)$
 5. Center: $(-3, 2)$
 Foci: $(-3 \pm \sqrt{2}, 2)$
 Vertices: $(-1, 2), (-5, 2)$
 7. Center: $(-5, 1)$
 Foci: $(-5, 1 \pm 2\sqrt{3})$
 Vertices: $(-5, 5), (-5, -3)$
 9. Center: $(-4, 2)$
 Foci: $(-4 \pm 3\sqrt{2}, 2)$
 Vertices: $(-4 \pm 3\sqrt{3}, 2)$

11. Center: $(2, 0)$
 Foci: $(4, 0), (0, 0)$
 Vertices: $(2 \pm \sqrt{5}, 0)$

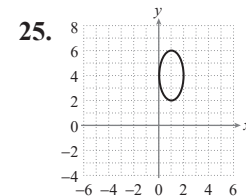
13. e 15. f
 17. c 19. b



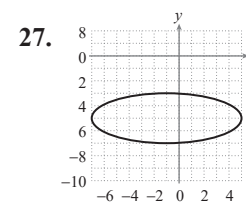
$(3 \pm 2\sqrt{2}, -1)$



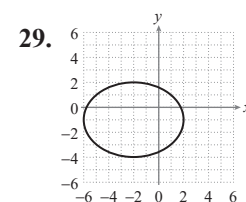
$(3 \pm \sqrt{5}, 4)$



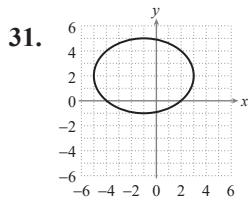
$(1, 4 \pm \sqrt{3})$



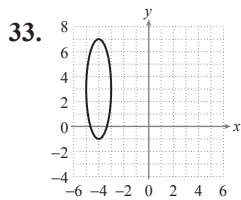
$(-1 \pm \sqrt{21}, -5)$



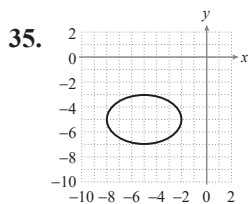
$(-2 \pm \sqrt{7}, -1)$



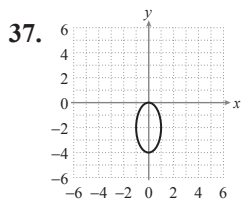
$$(-1 \pm \sqrt{7}, 2)$$



$$(-5, 3 \pm \sqrt{15})$$



$$(-5 \pm \sqrt{5}, -5)$$



$$(0, -2 \pm \sqrt{3})$$

39. $\frac{x^2}{16} + \frac{y^2}{25} = 1$

41. $(x-1)^2 + \frac{(y-1)^2}{9} = 1$

43. $\frac{(x-3)^2}{36} + \frac{y^2}{27} = 1$

45. $(x+2)^2 + \frac{(y+3)^2}{4} = 1$

47. $\frac{(x-5)^2}{16} + \frac{(y-3)^2}{15} = 1$

49. $\frac{(x-2)^2}{4} + \frac{(y+2)^2}{9} = 1$

51. $\frac{(x-1)^2}{9} + \frac{y^2}{16} = 1$

53. $e = \frac{\sqrt{11}}{6}$; major = 24; minor = 20

55. $e = \frac{2\sqrt{2}}{3}$; major = 12; minor = 4

57. $e = \frac{\sqrt{3}}{2}$; major = 4; minor = 2

59. $e = \frac{\sqrt{2}}{2}$; major = 4; minor = $2\sqrt{2}$

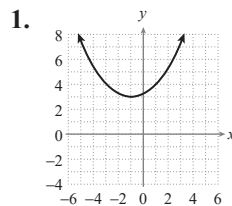
61. $e = \frac{\sqrt{42}}{7}$; major = 14;
minor = $2\sqrt{7}$

63. $e \approx 0.249$

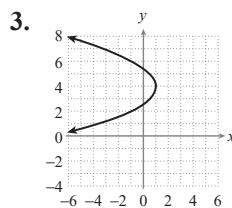
65. Yes, just barely, if the boat is centered on the river.

67. The string should be 5 cm long, and the tacks should be 4 cm apart.

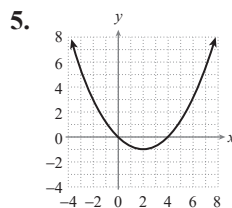
8.2 Exercises



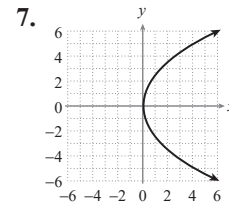
$$(-1, 4), y = 2$$



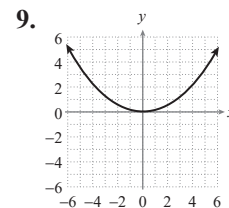
$$\left(\frac{1}{2}, 4\right), x = \frac{3}{2}$$



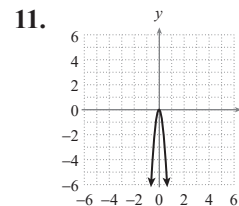
$$(2, 0), y = -2$$



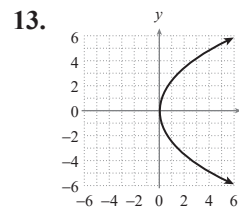
$$\left(\frac{3}{2}, 0\right), x = -\frac{3}{2}$$



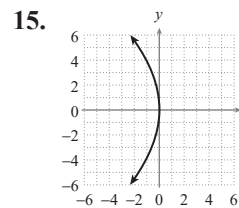
$$\left(0, \frac{7}{4}\right), y = -\frac{7}{4}$$



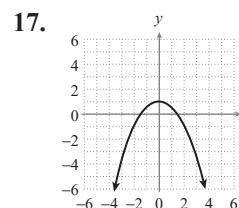
$$\left(0, -\frac{1}{48}\right), y = \frac{1}{48}$$



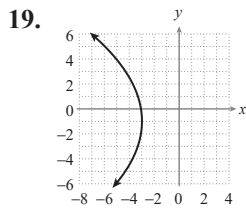
$$\left(\frac{3}{2}, 0\right), x = -\frac{3}{2}$$



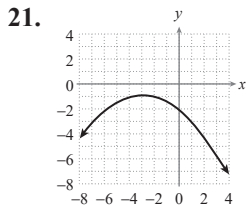
$$(-4, 0), x = 4$$



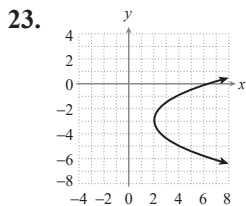
$$\left(0, \frac{1}{2}\right), y = \frac{3}{2}$$



$(-6, -1), x = 0$



$(-3, -3), y = 1$



$(\frac{5}{2}, -3), x = \frac{3}{2}$

25. g 27. b

29. e 31. d

33. $(y - 1)^2 = -4(x + 1)$

35. $(x - 3)^2 = 8(y + 1)$

37. $(y + 2)^2 = 24(x - 3)$

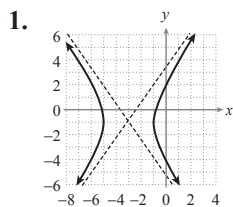
39. $(x + 3)^2 = -2(y + 1)$

41. $(y - 3)^2 = 10(x + 4)$

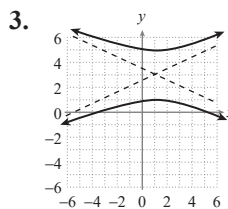
43. $(y + 1)^2 = -8(x - 2)$

45. 2 feet 47. 1.5 inches

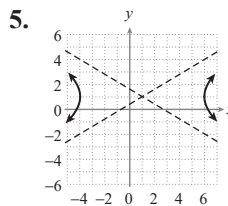
8.3 Exercises



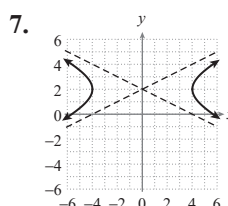
$(-3 \pm \sqrt{13}, -1)$



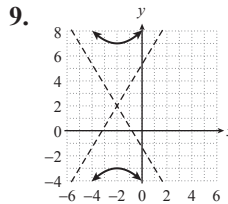
$(1, 3 \pm 2\sqrt{5})$



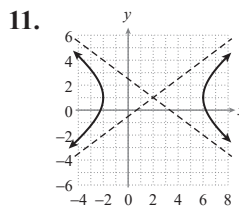
$(1 \pm \sqrt{34}, 1)$



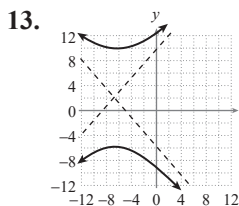
$(\pm 2\sqrt{5}, 2)$



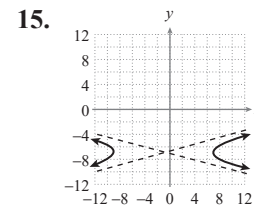
$(-2, 2 \pm \sqrt{34})$



$(7, 1), (-3, 1)$



$(-7, 2 \pm \sqrt{113})$



$(-1 \pm 2\sqrt{17}, -7)$

17. Center: $(-3, 2)$
Foci: $(-3 \pm \sqrt{13}, 2)$
Vertices: $(-1, 2), (-5, 2)$

19. Center: $(1, -4)$
Foci: $(1 \pm 2\sqrt{3}, -4)$
Vertices: $(1 \pm \sqrt{3}, -4)$

21. Center: $(-2, 1)$
Foci: $(-2 \pm \sqrt{30}, 1)$
Vertices: $(3, 1), (-7, 1)$

23. Center: $(-3, -1)$
Foci: $(-3 \pm 2\sqrt{3}, -1)$
Vertices: $(-1, -1), (-5, -1)$

25. Center: $(1, 0)$
Foci: $(1 \pm \frac{\sqrt{5}}{2}, 0)$
Vertices: $(2, 0), (0, 0)$

27. Center: $(8, 5)$
Foci: $(8 \pm 4\sqrt{5}, 5)$
Vertices: $(12, 5), (4, 5)$

29. a 31. b

33. g 35. h

37. $\frac{x^2}{4} - \frac{y^2}{5} = 1$

39. $y^2 - 4x^2 = 1$

41. $\frac{5x^2}{2} - \frac{5(y-4)^2}{18} = 1$

43. $\frac{(x-6)^2}{9} - \frac{(y-5)^2}{7} = 1$

45. $\frac{(x+4)^2}{4} - \frac{(y-3)^2}{16} = 1$

47. $\frac{(x-1)^2}{9} - \frac{(y+1)^2}{4} = 1$

49. $\frac{(y+4)^2}{16} - \frac{(x-3)^2}{25} = 1$

$$51. \frac{x^2}{(6 \times 10^7)^2} - \frac{y^2}{(7.2 \times 10^7)^2} = 1$$

Chapter 8 Project

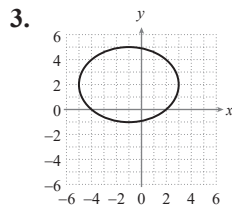
$$1. x^2 = -\frac{1125}{4}(y-80)$$

$$3. \frac{x^2}{22,500} + \frac{y^2}{6400} = 1, y \geq 0$$

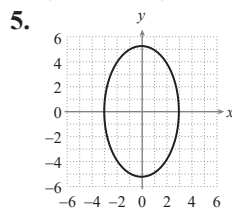
5. Answers may vary.
The semiellipse design, since it gives more space for ships to pass through.

Chapter 8 Review Exercises

1. Center: $(3, -1)$
Vertices: $(7, -1), (-1, -1)$
Foci: $(3 \pm 2\sqrt{3}, -1)$



$$(-1 \pm \sqrt{7}, 2)$$



$$(0, \pm 3\sqrt{2})$$

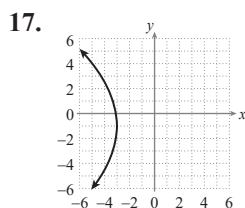
$$7. \frac{(x+1)^2}{9} + \frac{(y-4)^2}{16} = 1$$

$$9. \frac{4(x-2)^2}{9} + \frac{4(y+1)^2}{9} = 1$$

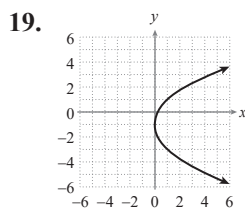
$$11. \frac{(x-2)^2}{16} + \frac{y^2}{12} = 1$$

$$13. \frac{(x+1)^2}{4} + \frac{(y-1)^2}{25} = 1$$

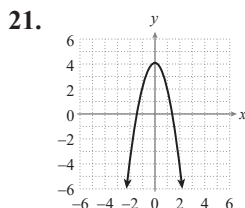
$$15. 30\pi a - \pi a^2$$



$$(-6, -1), x = 0$$



$$(1, -1), x = -1$$



$$\left(0, \frac{31}{8}\right), y = \frac{33}{8}$$

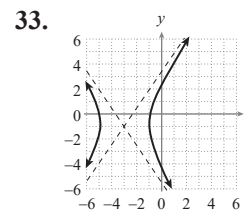
$$23. (x+2)^2 = 4(y-3)$$

$$25. (y+1)^2 = 2\left(x - \frac{5}{2}\right)$$

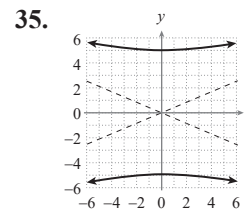
$$27. (y+1)^2 = 16(x-2)$$

$$29. (y+1)^2 = -16(x-5)$$

$$31. \frac{5}{4} \text{ inches}$$



$$(-3 \pm \sqrt{13}, -1)$$



$$(0, \pm 13)$$

$$37. \text{Center: } (0, 2)$$

$$\text{Foci: } (\pm 2\sqrt{10}, 2)$$

$$\text{Vertices: } (\pm 6, 2)$$

$$39. \text{Center: } (3, 3)$$

$$\text{Foci: } (3, 3 \pm \sqrt{53})$$

$$\text{Vertices: } (3, 1), (3, 5)$$

$$41. \frac{(x+1)^2}{4} - \frac{(y+2)^2}{25} = 1$$

$$43. \frac{(y-2)^2}{9} - \frac{(x-2)^2}{1} = 1$$

$$45. \frac{(y-7)^2}{4} - \frac{(x+1)^2}{9} = 1$$

$$47. \frac{(y+2)^2}{9} - \frac{x^2}{4} = 1$$

Chapter 9: Systems of Equations and Inequalities

9.1 Exercises

1. $(-5, 2)$ 3. $(5, 3)$

5. \emptyset

7. $\left\{ \left(\frac{y-3}{2}, y \right) \mid y \in \mathbb{R} \right\}$

9. $(-1, 7)$ 11. $(3, 11)$

13. $\{(x, 4x+1) \mid x \in \mathbb{R}\}$

15. $(2, 19)$ 17. $(-5, 1)$

19. $(5, 6)$

21. $\{(-y-2, y) \mid y \in \mathbb{R}\}$

23. $(-5, 4)$ 25. $(-1, 1)$

27. $(3, -5)$ 29. \emptyset

31. $(-1, 3, 0)$ 33. $(2, 2, -1)$

35. $\left\{ \left(\frac{y-z+2}{3}, y, z \right) \mid y \in \mathbb{R}, z \in \mathbb{R} \right\}$

37. \emptyset 39. $(1, 1, 0)$

41. $(9, 1, 1)$ 43. $(3, 1, -2)$

45. $(4, 5, 5)$ 47. $\left(\frac{49}{3}, \frac{-16}{3}, \frac{5}{4} \right)$

49. $(0, 3, 2)$

51. 22 pennies, 23 nickels

53. 25 people
 55. Eliza is 15 years old.
 57. 7 shirts and 4 pairs of shorts
 59. 3 quarters, 11 dimes, and 28 pennies
 61. Jim is 28 years old.
 63. 3 thumb screws
 65. Apples: \$0.78, Oranges: \$0.93, Mangoes: \$1.05
 67. (0.43, 1.28, 3.64)
 69. (-3.42, 2.98, 2.76)
 71. (6, 8, 7)

9.2 Exercises

1. a. 3×2 b. -1 c. None
 3. a. 5×2 b. None c. 10
 5. a. 3×4 b. None c. 286
 7. a. 3×2 b. 1 c. None
 9. a. 2×5 b. 5 c. 2

$$11. \left[\begin{array}{ccc|c} -3 & 1 & -2 & -4 \\ \frac{1}{2} & -4 & -1 & 1 \\ 0 & -3 & 3 & 1 \end{array} \right]$$

$$13. \left[\begin{array}{ccc|c} -\frac{3}{2} & -1 & 0 & -1 \\ 2 & 2 & 3 & 0 \\ 0 & -1 & 6 & 0 \end{array} \right]$$

$$15. \left[\begin{array}{ccc|c} \frac{12}{5} & \frac{1}{2} & -\frac{3}{2} & \frac{1}{5} \\ 1 & 0 & 3 & 1 \\ 5 & 2 & 1 & -2 \end{array} \right]$$

$$17. \left[\begin{array}{ccc|c} \frac{2}{3} & -\frac{4}{3} & -2 & 0 \\ 8 & -2 & 6 & 7 \\ 3 & -2 & 0 & 0 \end{array} \right]$$

$$19. \left[\begin{array}{ccc|c} \frac{1}{2} & -14 & -\frac{1}{4} & -8 \\ \frac{1}{5} & -\frac{7}{6} & \frac{1}{4} & -3 \\ 5 & -5 & \frac{8}{3} & -5 \end{array} \right]$$

$$21. \begin{cases} x = 8 \\ y = 3 \end{cases}$$

$$23. \begin{cases} x + 3y + 6z = 16 \\ y + 2z = 9 \\ z = 4 \end{cases}$$

$$25. \begin{cases} 9y + 13z = 27 \\ 2x + 21z = 19 \\ 7x + 18y = 32 \end{cases}$$

$$27. \left[\begin{array}{cc|c} 2 & -5 & 3 \\ 0 & -7 & 5 \end{array} \right]$$

$$29. \left[\begin{array}{cc|c} 1 & 3 & -2 \\ 9 & -2 & 7 \end{array} \right]$$

$$31. \left[\begin{array}{cc|c} 8 & -2 & -4 \\ -6 & 2 & -14 \end{array} \right]$$

$$33. \left[\begin{array}{cc|c} 4 & 12 & -6 \\ 9 & 9 & 6 \end{array} \right]$$

$$35. \left[\begin{array}{cc|c} 4 & -1 & 5 \\ -6 & 2 & 0 \end{array} \right]$$

$$37. \left[\begin{array}{ccc|c} 18 & -6 & 15 & 42 \\ -7 & 19 & 2 & 3 \\ -4.5 & 5.5 & -2 & 3.5 \end{array} \right]$$

$$39. \left[\begin{array}{ccc|c} 5 & 18 & 22 & 5 \\ 32 & -9 & -27 & -23 \\ -9 & 21 & 12 & 9 \end{array} \right]$$

$$41. \left[\begin{array}{ccc|c} 0 & 1 & -9 & -3 \\ 1 & 1 & 3 & 4 \\ 0 & 0 & 0 & 0 \end{array} \right]$$

$$43. \left[\begin{array}{cc|c} -1 & 4 & -3 \\ 1 & -6 & \frac{5}{2} \end{array} \right]$$

$$45. \left[\begin{array}{ccc|c} 1 & 5 & -9 & 11 \\ 0 & -1 & 8 & -7 \\ 0 & -17 & 41 & 1 \end{array} \right]$$

47. Neither 49. Neither

51. Neither 53. (3, -1)

55. (1, 3) 57. (-7, 3)

59. \emptyset 61. (3, 2)

63. $\{(-2y - 4, y) \mid y \in \mathbb{R}\}$

65. \emptyset 67. (4, 0, 3)

69. (15, -21, 8) 71. (3, -5)

73. $\{(x, -3x - 2) \mid x \in \mathbb{R}\}$

75. (-4, 1) 77. (6, 4)

79. (-11, -5) 81. (7, 3, 3)

83. (2, 2, -1)

85. $\{(1, y, 0) \mid y \in \mathbb{R}\}$

87. (3, -2, 3) 89. (2, 3, 4)

91. (9, -19, 7) 93. (1, -2, -1, 3)

95. 42, 26, 87

97. Small: 10, Medium: 24, Large: 48

9.3 Exercises

1. 11 3. 15

5. $ab - x^2$ 7. 8

9. -10 11. -39

13. $\{-2, 3\}$ 15. $\{-5, 1\}$

17. $\{-5, -4\}$ 19. $\{-6, 4\}$

21. $\{2, 5\}$ 23. 3

25. -9 27. 2

29. -2 31. 159

33. 78 35. -254

36. -84 37. 404

39. 4 41. 120

43. 10 45. x^4

47. x^8 49. (76, -53)

51. $\{(-y - 2, y) \mid y \in \mathbb{R}\}$

53. \emptyset

55. $\{(-3z - 5, -6z - 10, z) \mid z \in \mathbb{R}\}$

$$57. \left\{ \left(\frac{-5y - z - 5}{2}, \frac{-5y + 3z - 19}{2}, y, z \right) \mid \begin{array}{l} y \in \mathbb{R}, \\ z \in \mathbb{R} \end{array} \right\}$$

$$59. \left\{ \left(-z + 8, -5z + 31, -2z + 37, z \right) \mid z \in \mathbb{R} \right\}$$

61. (1647, 2071)

63. \emptyset

65. (-3, -1, 0, -4)

67. Candy bars: 5, Ice cream: 6

69. 0.012 71. 0.564

73. 1194 75. (1, -1, 2)

77. (2, 1, 0, 3)

9.4 Exercises

1. $\begin{bmatrix} 5 & -1 \\ 0 & 0 \\ 2 & 13 \end{bmatrix}$ 3. $\begin{bmatrix} 6 & -3 \\ 18 & 30 \\ -9 & 21 \end{bmatrix}$

5. Not possible 7. $\begin{bmatrix} 14 & -14 \\ 8 & 0 \\ -4 & 14 \end{bmatrix}$

9. $\begin{bmatrix} -7 & 5 \\ 3 & 10 \\ -3 & -8 \end{bmatrix}$ 11. Not possible

13. $a = 3, b = -1, c = 10$

15. $a = 2, b = -2, c = -1$

17. Not possible 19. $x = 10, y = 5$

21. $x = 3, y = 1$ 23. Not possible

25. $a = 8, b = 5$ 27. $[24 \ -5]$

29. $[35 \ 18]$ 31. Not possible

33. $[-30 \ -3]$

35. $\begin{bmatrix} 15 & -3 & -24 \\ 25 & -5 & -40 \\ 30 & -6 & -48 \end{bmatrix}$

37. $[-34 \ -7]$

39. $\begin{bmatrix} 11 & 0 \\ 0 & 11 \end{bmatrix}$

41. $\begin{bmatrix} 32 & -20 \\ 56 & -35 \\ -16 & 10 \end{bmatrix}$

43. Not possible

45. $\begin{bmatrix} 14 & -13 \\ -13 & 5 \end{bmatrix}$

47. $\begin{bmatrix} 179 & 76 \end{bmatrix}$

49. $\frac{2}{3}$ for store A; $\frac{1}{3}$ for store B

51. Solution is incorrect.

Explanations may vary.

53. $\begin{bmatrix} 23.94 & -7.56 & 28.98 \\ 21.66 & -6.84 & 26.22 \end{bmatrix}$

55. $[-23.94 \ -26.72]$

57. $\begin{bmatrix} -79.59 \\ 39.21 \\ 10.08 \end{bmatrix}$

9.5 Exercises

1. $\begin{bmatrix} 14 & -5 \\ 1 & 9 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 7 \\ 2 \end{bmatrix}$

3. $\begin{bmatrix} 1 & 2 \\ 9 & -3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -6 \\ -14 \end{bmatrix}$

5. $\begin{bmatrix} 3 & -7 & 1 \\ 1 & -1 & 0 \\ 0 & 8 & 5 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -4 \\ 2 \\ -3 \end{bmatrix}$

7. $\begin{bmatrix} 3 & -8 \\ 5 & -5 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 2 \\ 2 \end{bmatrix}$

9. $\begin{bmatrix} 4 & -3 \\ 2 & -4 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} -9 \\ 13 \end{bmatrix}$

11. $\begin{bmatrix} 2 & -1 & 3 \\ -1 & 1 & 0 \\ 4 & -5 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 0 \\ 17 \\ -2 \end{bmatrix}$

13. $\begin{bmatrix} -\frac{1}{20} & -\frac{1}{5} \\ \frac{1}{4} & 0 \end{bmatrix}$

15. $\begin{bmatrix} -5 & -4 \\ 4 & 3 \end{bmatrix}$

17. $\begin{bmatrix} -5 & 0 \\ 2 & 2 \end{bmatrix}$

19. Not invertible

21. $\begin{bmatrix} 2 & 1 & -4 \\ -4 & -2 & -3 \\ -1 & -1 & -4 \end{bmatrix}$

23. $\begin{bmatrix} -1 & 2 & -1 \\ 0 & -1 & 1 \\ 0 & -4 & 3 \end{bmatrix}$

25. $\begin{bmatrix} -1 & -2 & 1 \\ -2 & 1 & -3 \\ 1 & 2 & 0 \end{bmatrix}$

27. $\begin{bmatrix} -2 & 1 & 1 \\ 2 & 0 & -1 \\ -1 & 0 & 1 \end{bmatrix}$

29. $\begin{bmatrix} 2 & -1 & 2 \\ 0 & 1 & -1 \\ -3 & -2 & -4 \end{bmatrix}$

31. No

33. Yes

35. No

37. $\left(-2, -\frac{5}{2}\right)$

39. $\left\{\left(\frac{3y-1}{2}, y\right) \mid y \in \mathbb{R}\right\}$

41. (-2, 0) 43. (8, -19)

45. (0, 5) 47. (-4, 5, -1)

49. (-13, 19, 23); (0, 0, -1); (1, -1, -1)

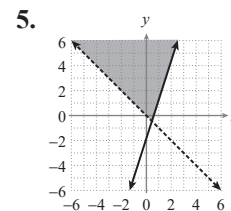
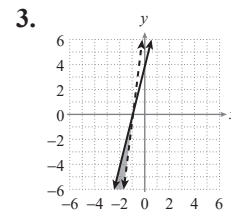
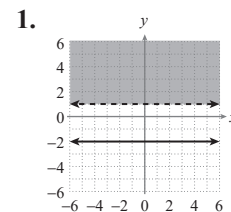
51. (1, -8, 7); (3, 1, 1); (4, 2, 0)

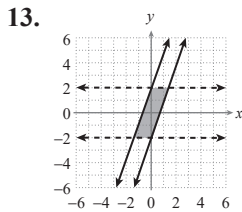
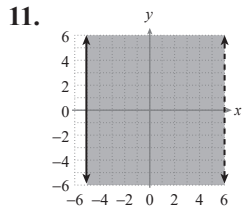
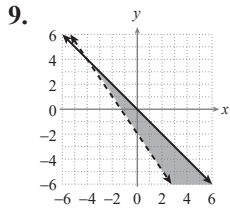
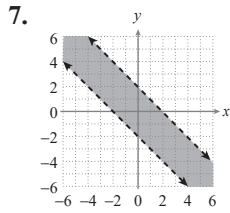
53. $\begin{bmatrix} -\frac{1}{4} & \frac{1}{10} \\ -\frac{1}{4} & \frac{3}{10} \end{bmatrix}$

55. $\begin{bmatrix} 0.053 & -0.258 \\ 0.113 & 0.076 \end{bmatrix}$

57. $\begin{bmatrix} 0.004 & -0.003 & 0.009 \\ 0 & 0.020 & 0.029 \\ 0.012 & 0.014 & 0.013 \end{bmatrix}$

9.6 Exercises





15. Min = 0 at (0, 0);
Max = 12 at (3, 0)

17. Min = 0 at (0, 0);
Max = 12 at (0, 3)

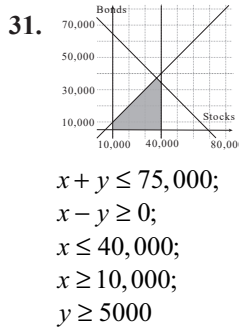
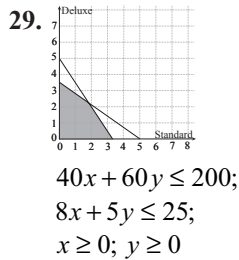
19. Min = 100 at $(\frac{10}{3}, 10)$;
Max = 250 at (20, 10)

21. Min = $\frac{150}{7}$ at $(\frac{50}{7}, 0)$;
Max = 66 at (8, 6)

23. Min = 0 at (0, 0);
Max = $\frac{165}{8}$ at $(\frac{111}{8}, \frac{27}{8})$

25. Min = 210 at (14, 0);
Max = 600 at (0, 20)

27. Min = $\frac{680}{7}$ at $(\frac{88}{7}, \frac{-36}{7})$;
Max = $\frac{1980}{7}$ at $(\frac{108}{7}, \frac{-6}{7})$



33. Type X: 75 units;
Type Y: 100 units;
Maximum profit: \$712.50

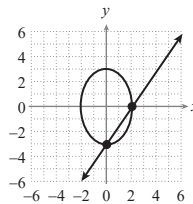
35. The volunteer could choose any of the following points: (9, 9), (11, 6), (13, 3), (15, 0). In each of these points, the first coordinate represents the number of packages from Company A and the second coordinate represents the number of packages from Company B. The minimum cost is \$22.50.

37. a. 120 flip phones;
80 smart phones;
Minimum cost: \$1160

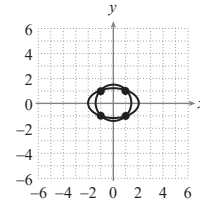
b. 100 flip phones;
170 smart phones;
Maximum profit: \$650

9.7 Exercises

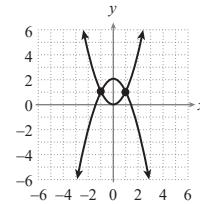
1. $\{(0, -3), (2, 0)\}$



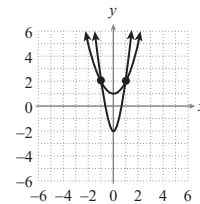
3. $\{(-1, -1), (1, 1)\}$
 $\{(-1, 1), (1, -1)\}$



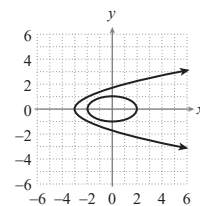
5. $\{(-1, 1), (1, 1)\}$



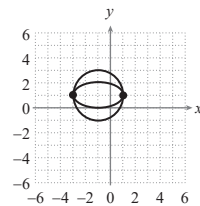
7. $\{(-1, 2), (1, 2)\}$



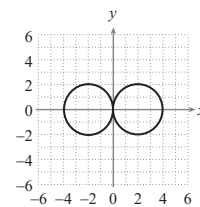
9. No solution



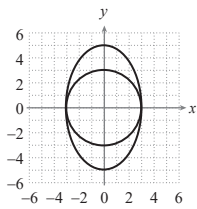
11. $\{(-3, 1), (1, 1)\}$



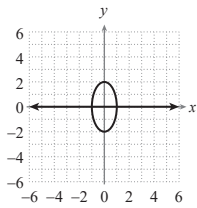
13. $\{(0, 0)\}$



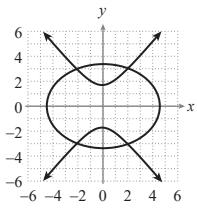
15. $\{(\pm 3, 0)\}$



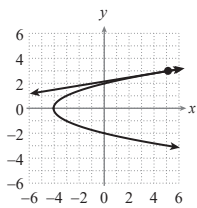
17. $\{(\pm 1, 0)\}$



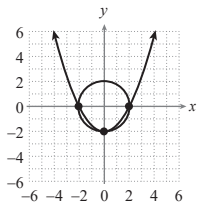
19. $\{(2, \pm 3), (-2, \pm 3)\}$



21. $\{(5, 3)\}$



23. $\{(\pm 2, 0), (0, -2)\}$



25. $\left\{ \begin{matrix} (-i\sqrt{6}, -6), (i\sqrt{6}, -6), \\ (-\sqrt{5}, 5), (\sqrt{5}, 5) \end{matrix} \right\}$

27. $\{(-2, 3)\}$

29. $\left\{ \begin{matrix} (-1, -4), (1, 4), (-2\sqrt{2}, -\sqrt{2}), \\ (2\sqrt{2}, \sqrt{2}) \end{matrix} \right\}$

31. $\{(-3i, -5), (3i, -5), (0, 4)\}$

33. $\{(-\sqrt{3}, 0), (\sqrt{3}, 0)\}$

35. $\{(-i, -6), (i, -6), (-\sqrt{2}, 3), (\sqrt{2}, 3)\}$

37. $\left\{ \begin{matrix} (1, 1), \left(-\frac{3}{2}, \frac{\sqrt{14}}{2}\right), \\ (1, -1), \left(-\frac{3}{2}, -\frac{\sqrt{14}}{2}\right) \end{matrix} \right\}$

39. $\left\{ \left(\frac{7}{2}, \frac{17}{4}\right) \right\}$

41. $\left\{ \begin{matrix} (-6, -i\sqrt{15}), (2, 1), \\ (-6, i\sqrt{15}), (2, -1) \end{matrix} \right\}$

43. $\left\{ \left(0, 1\right), \left(-\frac{100}{101}, -\frac{99}{101}\right) \right\}$

45. $\left\{ \begin{matrix} \left(-\frac{\sqrt{42}}{6}, -\frac{\sqrt{66}}{6}\right), \\ \left(-\frac{\sqrt{42}}{6}, \frac{\sqrt{66}}{6}\right), \\ \left(\frac{\sqrt{42}}{6}, -\frac{\sqrt{66}}{6}\right), \\ \left(\frac{\sqrt{42}}{6}, \frac{\sqrt{66}}{6}\right) \end{matrix} \right\}$

47. $\{(-5, 0), (-2, 0), (-1, 0)\}$

49. $\left\{ \begin{matrix} (3, 2), (2, 3), \\ \left(\frac{-1 \pm i\sqrt{23}}{2}, \frac{-1 \pm i\sqrt{23}}{2}\right) \end{matrix} \right\}$

51. $\left\{ \left(0, -1\right), \left(\frac{\sqrt{6}}{3}, \frac{2\sqrt{6}}{9} - 1\right) \right\}$

53. $\left\{ \begin{matrix} (\sqrt{2} + 1, 2\sqrt{2}), (-\sqrt{2} + 1, -2\sqrt{2}), \\ (2\sqrt{2} + 1, \sqrt{2}), (-2\sqrt{2} + 1, -\sqrt{2}) \end{matrix} \right\}$

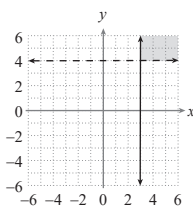
55. $\{(4, 1), (1, 1 + i\sqrt{3})\}$

57. $\{(0, 4), (0, -3), (3, -2), (3, 3)\}$

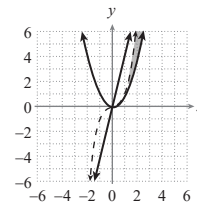
59. $\{(4, 0)\}$

61. $\left\{ \left(\pm \frac{1}{2}, \pm \frac{1}{4}\right) \right\}$

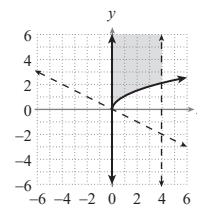
63. b



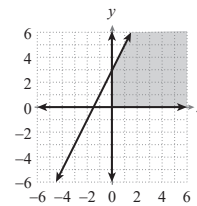
65. b, d



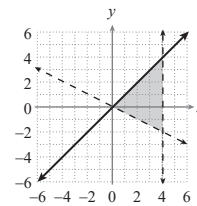
67. a, d



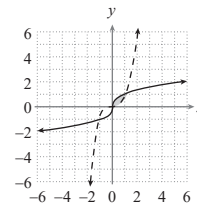
69.



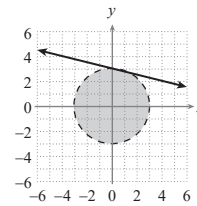
71.



73.



75.



77. 9 inches by 5 inches

79. 60 mph and 70 mph

81. -12 and 7

83. $h = 6$ cm, $r = 3$ cm

Chapter 9 Project

1.

The number of months passed	Shop Name		
	Joe's Java	Buck's Café	Tweak's Coffee
1	26.85%	43.45%	29.70%
2	28.47%	42.10%	29.43%
3	29.88%	40.92%	29.20%
4	31.12%	39.89%	28.98%
5	32.21%	39.00%	28.80%
6	33.16%	38.21%	28.63%

3. As our market share increases, the shares of both Buck's Café and Tweak's Coffee decrease. As such, they will have to adjust their marketing strategies to stop the decrease and potentially increase their shares.

Chapter 9 Review Exercises

1. \emptyset 3. $(3, 0, 2)$
 5. \emptyset
 7. $\{(3-3y, y) | y \in \mathbb{R}\}$
 9. $(3, 2)$ 11. $(8, 12, 10)$

13. $y = \frac{4}{15}x^2 - x + \frac{11}{15}$

15. a. 1×4 b. 8 c. None

17. $\left[\begin{array}{ccc|c} 4 & 5 & -1 & 0 \\ 1 & 3 & 2 & 3 \\ 10 & -1 & -6 & 0 \end{array} \right]$

19. $\begin{cases} 8x + 7z = 5 \\ -3y + 4z = 16 \\ 16x - 2y + z = 2 \end{cases}$

21. $\left[\begin{array}{cc|c} 0 & -5 & -11 \\ 1 & 2 & 3 \end{array} \right]$

23. $\left[\begin{array}{cc|c} 1 & -4 & -4 \\ 1 & 7 & 11 \end{array} \right]$

25. $(2, -1)$ 27. $(3, -5)$

29. $2x^4$ 31. 7

33. $9, -9$ 35. $(-4, 1)$

37. \emptyset

39. $\left[\begin{array}{ccc} 4 & -16 & 4 \\ -5 & 8 & 12 \end{array} \right]$

41. Not possible 43. $\begin{bmatrix} 9 & -23 & 3 \\ 5 & -3 & 8 \end{bmatrix}$

45. $w = -2, x = 1, y = 3, z = -4$

47. $x = 2, y = -3$

49. $[12 \ 46]$

51. $\begin{bmatrix} 1 & -1 & 2 \\ 2 & -3 & -1 \\ -3 & 0 & 6 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix} = \begin{bmatrix} -4 \\ 1 \\ 5 \end{bmatrix}$

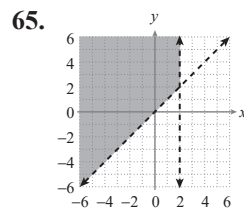
53. $\begin{bmatrix} 3 & 1 \\ 16 & 8 \\ -1 & 1 \\ 8 & 4 \end{bmatrix}$

55. Not possible

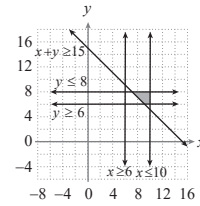
57. No 59. Yes

61. $\left(1, -\frac{1}{3}\right)$

63. $(-15, 20, -33), (-2, 3, -4), (-9, 11, -17)$



67. $x \geq 6, y \geq 6, x \leq 10, y \leq 8, x + y \geq 15$

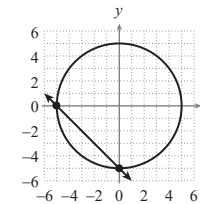


69. Min = 20 at $(0, 10)$
 Max = 50 at $(10, 0)$

71. Min = 350 at $(5, 0)$
 Max = 1028 at $(10, 4)$

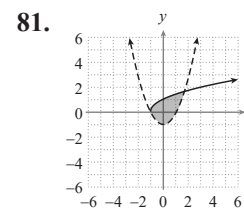
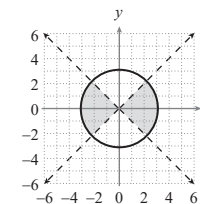
73. 35 bionic arms, 15 bionic legs,
 Min cost: \$24,000

75. $\{(-5, 0), (0, -5)\}$



77. $\{(4, 3), (-4, 3), (-4, -3), (4, -3)\}$

79. None



83. 9 and 16

Chapter 10: Sequences, Series, Combinatorics, and Probability

10.1 Exercises

1. Infinite 5. Finite
 3. Finite 9. Infinite
 7. Infinite

11. $2, -1, -4, -7, -10$

13. $1, \frac{3}{2}, \frac{9}{5}, 2, \frac{15}{7}$

15. $\frac{2}{3}, -\frac{4}{9}, \frac{8}{27}, -\frac{16}{81}, \frac{32}{243}$

17. $\frac{1}{2}, \frac{4}{3}, \frac{9}{4}, \frac{16}{5}, \frac{25}{6}$

19. $-1, 3, -6, 10, -15$

21. $26, 7, 0, -1, -2$

23. $-1, \sqrt{2}, -\sqrt{3}, 2, -\sqrt{5}$

25. 1, 5, 9, 13, 17

27. $\frac{1}{2}, 1, 2, 4, 8$

29. 3, 36, 729, 20, 736, 759, 375

31. $\frac{5}{4}, 2, \frac{5}{2}, \frac{20}{7}, \frac{25}{8}$

33. 1, 3, 6, 10, 15

35. Undefined, 9, 4, $\frac{25}{9}, \frac{9}{4}$

37. $\frac{1}{3}, \frac{1}{2}, \frac{5}{9}, \frac{7}{12}, \frac{3}{5}$

39. 0, -1, -4, -9, -16

41. 2, 4, 16, 256, 65, 536

43. 1, 2, 6, 24, 120

45. $2, \sqrt{5}, \sqrt{6}, \sqrt{7}, 2\sqrt{2}$

47. 1, 0, -27, 0, 125

49. $a_n = 7n - 2$

51. $a_1 = -1, a_n = -na_{n-1}, n \geq 2$

53. $a_n = \left(\frac{1}{n}\right)^2$

55. $a_n = 9n - 43$

57. $a_n = 2^{n-3}$

59. $a_n = \frac{n}{2^n}$

61. $-2 + 1 + 4 + 7 + 10 + 13 + 16 = 49$

63. $\sum_{i=1}^6 i^3 = 441$

65. $45 + 80 + 125 + 180 + 245 + 320 + 405 + 500 = 1900$

67. $-6 - 12 - 24 - 48 - 96 - 192 = -378$

69. $\sum_{i=2}^9 3^i = 29,520$

71. $S_n = \frac{n}{4(n+4)}, S = \frac{1}{4}$

73. $S_n = 2^n - 1, S_{15} = 32,767$

75. $S_n = \frac{n}{2(n+1)}, S = \frac{1}{2}$

77. $S_n = -\ln(n+1)$, series diverges

79. $S_n = \frac{3n}{4(3n+4)}, S = \frac{1}{4}$

81. 4, 7, 11, 18, 29

83. 10, 20, 30, 50, 80

85. 13, -17, -4, -21, -25

87. 1, -3, -3, 9, -27

89. 987

91. 1, 2, 4, 8, 16, 32, 64, 128

10.2 Exercises

1. $a_n = 3n - 5$

3. $a_n = -2n + 9$

5. $a_n = 9n - 4$

7. $a_n = -6n + 9$

9. $a_n = 19n + 5$

11. $a_n = n + \frac{5}{2}$

13. $a_n = -\frac{19}{2}n + \frac{43}{2}$

15. $a_n = -2n + 1$

17. $a_n = -4n + 33$

19. $d = 2$ 21. $d = 1$ 23. No

25. No 27. 13 29. 2

31. 2

33. $d = 2.5; 5, 7.5, 10, 12.5, 15$

35. $d = 7; 7, 14, 21, 28, 35$

37. $d = 9; -62, -53, -44, -35, -26$

39. $d = 5$ 41. $d = 1$ 43. $d = -2$

45. 195 47. a_{73} 49. 117

51. 26 53. -8 55. 13

57. 55 59. 14,350

61. 17,114 63. -1475

65. $-\frac{3219}{5}$ 67. 902

69. -1316 71. 6 years

73. 1620 pounds

75. \$625; \$8100

77. 266.4

79. -152

81. 10,382.05

10.3 Exercises

1. $a_n = -3(2)^{n-1}$

3. $a_n = 2\left(-\frac{1}{3}\right)^{n-1}$

5. $a_n = \left(-\frac{1}{4}\right)^{n-1}$

7. $a_n = \left(\frac{1}{7}\right)^{n-1}$

9. $a_n = (-3)^{n-1}$

11. $a_n = 3\left(\frac{2}{3}\right)^{n-1}$

13. $a_n = 7(-2)^{n-1}$

15. $a_n = \frac{1}{16}(2)^{n-1}$

17. $a_n = \frac{39}{68}\left(\frac{4}{3}\right)^{n-1}$

19. No 21. $r = \frac{1}{2}$ 23. $r = 2$

25. $r = 7$

27. $r = 3; 8, 24, 72, 216, 648$

29. $r = 2; \frac{1}{4}, \frac{1}{2}, 1, 2, 4$

31. $r = \frac{1}{5};$

62,500, 12,500, 2500, 500, 100

33. $\frac{5}{16,384}$

35. -2,147,483,648

37. $r = \pm 2$ 39. $r = \pm \frac{1}{5}$

41. $\frac{52,222,139,775}{1,048,576} \approx 49,802.9$

43. $\frac{10,923}{16,384} \approx 0.666687$

45. $\frac{73,810}{19,683} \approx 3.749936$

47. -109,200

49. $-\frac{3}{2}$

51. Series diverges

53. $\frac{2,476,099}{160,000} \approx 15.475619$

55. Series diverges

57. $\frac{28,561}{152,064} \approx 0.187822$

59. $\frac{123}{999}$ 61. $-\frac{35}{9}$ 63. $\frac{989}{99}$

65. \$14,802.44 67. 1.845×10^{19}

69. Approximately 13,778 students

71. $S_{30} = 1.1 \times 10^{30}; r = 10$

73. Yes; explanations will vary (any example such that $r = 1$ and $d = 0$).

75. 9.98

77. 2.137×10^{-18}

79. 6.54×10^{51}

10.4 Exercises

1. $S_{k+1} = \frac{1}{3k+9}$

3. $S_{k+1} = \frac{(k+1)(k+2)(2k+3)}{4}$

5. Basic Step:

$$n = 1, 1 = 1 \text{ and } \frac{1(1+1)}{2} = 1;$$

Induction Step:

$$\text{If } 1 + 2 + 3 + \dots + k = \frac{k(k+1)}{2},$$

then $(1 + 2 + 3 + \dots + k) + (k + 1)$

$$= \frac{k(k+1)}{2} + (k+1)$$

$$= \frac{k^2 + k + 2k + 2}{2}$$

$$= \frac{(k+1)(k+2)}{2}$$

7. Basic Step:

$$n = 1, 2(1) = 2 \text{ and } 1(1+1) = 2;$$

Induction Step:

$$\text{If } 2 + 4 + 6 + \dots + 2k = k(k+1),$$

then

$$(2 + 4 + 6 + \dots + 2k) + 2(k+1)$$

$$= k^2 + k + 2k + 2$$

$$= (k+1)(k+2)$$

9. Basic Step:

$$n = 1, 4^{1-1} = 1 \text{ and } \frac{4^1 - 1}{3} = 1;$$

Induction Step:

$$\text{If } 4^0 + 4^1 + 4^2 + \dots + 4^{k-1} = \frac{4^k - 1}{3},$$

$$\text{then } 4^0 + 4^1 + 4^2 + \dots + 4^{k-1} + 4^{k+1-1}$$

$$= \frac{4^k - 1}{3} + 4^k = \frac{4^k - 1 + 3 \cdot 4^k}{3}$$

$$= \frac{4 \cdot 4^k - 1}{3} = \frac{4^{k+1} - 1}{3}$$

11. Basic Step:

$$n = 1, \frac{1}{(3(1)-2)(3(1)+1)} = \frac{1}{4}$$

$$\text{and } \frac{1}{3(1)+1} = \frac{1}{4};$$

Induction Step:

$$\text{If } \frac{1}{1 \cdot 4} + \frac{1}{4 \cdot 7} + \frac{1}{7 \cdot 10}$$

$$+ \dots + \frac{1}{(3k-2)(3k+1)} = \frac{k}{3k+1},$$

$$\text{then } \frac{1}{1 \cdot 4} + \frac{1}{4 \cdot 7} + \frac{1}{7 \cdot 10}$$

$$+ \dots + \frac{1}{(3k-2)(3k+1)}$$

$$+ \frac{1}{(3(k+1)-2)(3(k+1)+1)}$$

$$= \left[\frac{1}{1 \cdot 4} + \frac{1}{4 \cdot 7} + \frac{1}{7 \cdot 10} + \dots + \frac{1}{(3k-2)(3k+1)} \right]$$

$$+ \frac{1}{(3k+1)(3k+4)}$$

$$= \frac{k}{3k+1} + \frac{1}{(3k+1)(3k+4)}$$

$$= \frac{3k^2 + 4k + 1}{(3k+1)(3k+4)}$$

$$= \frac{(3k+1)(k+1)}{(3k+1)(3k+4)} = \frac{(k+1)}{(3(k+1)+1)}$$

13.

Basic Step:

$$n = 1, 5(1) = 5 \text{ and } \frac{5(1)(1+1)}{2} = 5;$$

Induction Step:

$$\text{If } 5 + 10 + 15 + \dots + 5k = \frac{5k(k+1)}{2},$$

$$\text{then } 5 + 10 + 15 + \dots + 5k + 5(k+1)$$

$$= (5 + 10 + 15 + \dots + 5k) + 5k + 5$$

$$= \frac{5k(k+1)}{2} + 5k + 5$$

$$= \frac{5k^2 + 15k + 10}{2}$$

$$= \frac{5(k+1)(k+2)}{2}$$

$$= \frac{5(k+1)[(k+1)+1]}{2}$$

15.

Basic Step:

$$n = 1, 1 + \frac{1}{1} = 2 \text{ and } 1 + 1 = 2$$

Induction Step:

$$\text{If } \left(1 + \frac{1}{1}\right)\left(1 + \frac{1}{2}\right)\left(1 + \frac{1}{3}\right) \dots \left(1 + \frac{1}{k}\right) = k + 1,$$

then

$$\left(1 + \frac{1}{1}\right)\left(1 + \frac{1}{2}\right)\left(1 + \frac{1}{3}\right) \dots \left(1 + \frac{1}{k}\right)\left(1 + \frac{1}{k+1}\right)$$

$$= (k+1)\left(1 + \frac{1}{k+1}\right)$$

$$= k+1 + \frac{k+1}{k+1} = (k+1)+1$$

17.

Basic Step:

$$n = 1, 3(1) - 2 = 1 \text{ and } \frac{1}{2}(3(1) - 1) = 1;$$

Induction Step:

$$\text{If } 1 + 4 + 7 + 10 + \dots + (3k-2) = \frac{k}{2}(3k-1),$$

then

$$[1 + 4 + 7 + 10 + \dots + (3k-2)]$$

$$+ [3(k+1) - 2]$$

$$= \frac{k}{2}(3k-1) + (3k+1)$$

$$= \frac{k(3k-1) + 2(3k+1)}{2}$$

$$= \frac{3k^2 + 5k + 2}{2}$$

$$= \frac{(k+1)(3k+2)}{2}$$

$$= \frac{k+1}{2}(3(k+1)-1)$$

19. Basic Step:

$$n = 2, 3^2 = 9 \text{ and } 2(2) + 1 = 5,$$

$$\text{so } 3^2 > 2(2) + 1;$$

Induction Step:

$$\text{If } 3^k > 2k + 1, \text{ then}$$

$$3^{k+1} = 3^1 \cdot 3^k > 3(2k+1)$$

$$= 6k + 3 > 2k + 3$$

$$= 2k + 2 + 1 = 2(k+1) + 1$$

21.

Basic Step:

$$n=1, 1^3=1 \text{ and } \frac{1^2(1+1)^2}{4}=1;$$

Induction Step:

$$\text{If } 1^3+2^3+3^3+4^3+\dots+k^3=\frac{k^2(k+1)^2}{4},$$

then

$$\begin{aligned} & (1^3+2^3+3^3+4^3+\dots+k^3)+(k+1)^3 \\ &= \frac{k^2(k+1)^2}{4} + (k+1)^3 \\ &= \frac{k^2(k+1)^2+4(k+1)^3}{4} \\ &= \frac{(k+1)^2(k+2)^2}{4} = \frac{(k+1)^2((k+1)+1)^2}{4} \end{aligned}$$

23. Basic Step:

$$n=1, a^1 = a \text{ so } a^1 > 1, \text{ when } a > 1;$$

Induction Step:

If $a^k > 1$, then

$$a^{k+1} = a^k \cdot a^1 > 1 \cdot a = a > 1$$

25.

Basic Step:

$$n=1, 1^4=1 \text{ and}$$

$$\frac{1(1+1)(2(1)+1)(3(1)^2+3(1)-1)}{30} = 1;$$

Induction Step:

$$\text{If } 1^4+2^4+3^4+\dots+k^4$$

$$= \frac{k(k+1)(2k+1)(3k^2+3k-1)}{30},$$

then

$$\begin{aligned} & (1^4+2^4+3^4+\dots+k^4)+(k+1)^4 \\ &= \frac{k(k+1)(2k+1)(3k^2+3k-1)}{30} + (k+1)^4 \\ &= \frac{6k^5+45k^4+130k^3+180k^2+119k+30}{30} \\ &= \frac{(k+1)(k+2)(2k+3)(3k^2+9k+5)}{30} \\ &= \frac{[(k+1)(k+2)(2(k+1)+1)] \times [3(k+1)^2+3(k+1)-1]}{30} \end{aligned}$$

27.

Basic Step:

$$n=2, \frac{1}{\sqrt{1}} + \frac{1}{\sqrt{2}} = 1 + \frac{\sqrt{2}}{2}$$

$$\text{and } 1 + \frac{\sqrt{2}}{2} > \sqrt{2};$$

Induction Step:

$$\text{If } \frac{1}{\sqrt{1}} + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} + \dots + \frac{1}{\sqrt{k}} > \sqrt{k},$$

then

$$\begin{aligned} & \left[\frac{1}{\sqrt{1}} + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{3}} + \dots + \frac{1}{\sqrt{k}} \right] + \frac{1}{\sqrt{k+1}} \\ & > \sqrt{k} + \frac{1}{\sqrt{k+1}} = \frac{\sqrt{k}(\sqrt{k+1})+1}{\sqrt{k+1}} \\ &= \frac{\sqrt{k^2+k+1}}{\sqrt{k+1}} > \frac{\sqrt{k^2+1}}{\sqrt{k+1}} \\ &= \frac{k+1}{\sqrt{k+1}} = \sqrt{k+1} \end{aligned}$$

29. Basic Step:

$$n=1, (ab)^1 = ab \text{ and } a^1 b^1 = ab;$$

Induction Step:

$$\text{If } (ab)^k = a^k b^k, \text{ then}$$

$$\begin{aligned} (ab)^{k+1} &= (ab)^k \cdot (ab) \\ &= a^k b^k \cdot ab = (a \cdot a^k)(b \cdot b^k) \\ &= a^{k+1} b^{k+1} \end{aligned}$$

31.

Basic Step:

$$n=1, \ln(x_1) = \ln x_1;$$

Induction Step:

$$\text{If } \ln(x_1 \cdot x_2 \cdot x_3 \cdots x_k)$$

$$= \ln x_1 + \ln x_2 + \ln x_3 + \dots + \ln x_k$$

$$\text{when } x_1 > 0, x_2 > 0, \dots, x_n > 0,$$

$$\text{then } \ln(x_1 \cdot x_2 \cdot x_3 \cdots x_k \cdot x_{k+1})$$

$$= \ln(x_1 \cdot x_2 \cdot x_3 \cdots x_k) + \ln(x_{k+1})$$

$$= (\ln x_1 + \ln x_2 + \ln x_3 + \dots + \ln x_k) + \ln x_{k+1}$$

33.

Basic Step: $n=2$,

$$(9^2 - 8(2) - 1) = 64 \text{ of which } 64 \text{ is a factor;}$$

Induction Step:

$$\text{If } (9^k - 8k - 1) = 64p \text{ for some integer } p,$$

$$\text{then } (9^{k+1} - 8(k+1) - 1)$$

$$= 9 \cdot 9^k - 8k - 9$$

$$= 9 \cdot 9^k - 9 \cdot 8k + 8 \cdot 8k - 9$$

$$= 9(9^k - 8k - 1) + 64k$$

$$= 9(64p) + 64k = 64(9p + k)$$

35.

Basic Step: $n=1$,

$$(1^3 - 1 + 3) = 3, \text{ which is divisible by } 3;$$

Induction Step:

$$\text{If } \frac{k^3 - k + 3}{3} = p$$

$$\text{or } k^3 - k + 3 = 3p \text{ for some integer } p,$$

$$\text{then } (k+1)^3 - (k+1) + 3$$

$$= k^3 + 3k^2 + 2k + 3$$

$$= (k^3 - k + 3) + (3k^2 + 3k)$$

$$= 3p + 3(k^2 + k) = 3(p + k^2 + k)$$

37.

Basic Step: $n=1$,

$$1(1+1)(1+2) = 6, \text{ which is divisible by } 6;$$

Induction Step:

$$\text{If } \frac{k(k+1)(k+2)}{6} = p$$

$$\text{or } k(k+1)(k+2) = 6p$$

for some integer p , then

$$(k+1)(k+2)(k+3)$$

$$= k^3 + 6k^2 + 11k + 6$$

$$= (k^3 + 3k^2 + 2k) + (3k^2 + 9k + 6)$$

$$= k(k+1)(k+2) + 3(k+1)(k+2)$$

$$= 6p + 3(k+1)(k+2).$$

$6p$ is clearly divisible by 6.

In order for $3(k+1)(k+2)$ to be

divisible by 6, it must be divisible

by 2 and 3. It is clearly divisible by 3.

If k is odd, then the term $(k+1)$ must

be even, making it divisible by 2.

If k is even, then the term $(k+2)$ is

even, making it divisible by 2.

Therefore, $3(k+1)(k+2)$ is divisible by 6.

39.

$$0+1+2+3+\dots+(n-1) = \frac{n(n-1)}{2};$$

Basic Step:

$$n=1, (1-1) = 0 \text{ and } \frac{1(1-1)}{2} = 0;$$

Induction Step:

$$\text{If } 0+1+2+\dots+(k-1) = \frac{k(k-1)}{2},$$

then

$$[0+1+2+\dots+(k-1)] + (k+1-1)$$

$$= \frac{k(k-1)}{2} + k = \frac{k^2 - k + 2k}{2}$$

$$= \frac{k(k+1)}{2} = \frac{(k+1)((k+1)-1)}{2}$$

41. The induction step does not work for $n = 1$. In the case of $n = 1$, $n + 1 = 2$ and the groups formed by removing the first horse and then the last horse do not overlap.

10.5 Exercises

1. combination
3. combination
5. 12 7. 720
9. 15 11. 792
13. $\frac{5!}{2!} = 60$
15. $\frac{7!}{2!2!} = 1260$
17. $\frac{11!}{2!2!2!} = 4,989,600$
19. $243x^5 + 405x^4y + 270x^3y^2 + 90x^2y^3 + 15xy^4 + y^5$
21. $x^4 - 12x^3 + 54x^2 - 108x + 81$
23. $7776x^{10} + 6480x^8y + 2160x^6y^2 + 360x^4y^3 + 30x^2y^4 + y^5$
25. $2401x^8 + 10,976x^6y^2 + 18,816x^4y^4 + 14,336x^2y^6 + 4096y^8$
27. $x^2 + 2xy + 2xz + y^2 + 2yz + z^2$
29. $64x^6 + 960x^5 + 6000x^4 + 20,000x^3 + 37,500x^2 + 37,500x + 15,625$
31. 32
33. $x^{16} + 48x^{15}y + 1080x^{14}y^2 + 15,120x^{13}y^3$
35. $129,140,163x^{\frac{17}{4}} + 3,658,971,285x^4y$
37. $651,168x^5$
39. $10^3 = 1000$
41. $9^7 = 4,782,969$
43. $15! \approx 1.308 \times 10^{12}$
45. $3! = 6$
47. $5^{10} = 9,765,625$
49. $36^6 = 2,176,782,336$
51. $26 \cdot 25 \cdot 24 \cdot 10 \cdot 9 \cdot 8 = 11,232,000$

53. ${}_{30}P_{12} \approx 4.143 \times 10^{16}$
55. ${}_{36}P_8 \approx 1.220 \times 10^{12}$
57. ${}_7P_6 = 5040$
 ${}_7P_7 = 5040$ as well. (Having a child remain standing is numerically equivalent to putting a seventh chair in the room.)

59. ${}_{26}P_3 = 15,600$
61. ${}_7C_3 = 35$
63. ${}_9C_2 = 36$
65. ${}_{75}C_5 = 17,259,390$
67. ${}_{10}C_4 \cdot {}_8C_4 \cdot {}_{13}C_4 = 10,510,500$

69. 112 cones
71. 96 outfits
73. 288 schedules
75. 120 5-letter strings
77. 303,600 ways
79. 495 pizzas
81. 752,538,150 groups
83. 420 ways

$$85. \binom{n}{n-k} = \frac{n!}{(n-k)!(n-(n-k))!} = \frac{n!}{(n-k)!(n-n+k)!} = \frac{n!}{(n-k)!k!} = \binom{n}{k}$$

$$87. 2^n = (1+1)^n = \sum_{k=0}^n \binom{n}{k} (1)^k (1)^{n-k} = \sum_{k=0}^n \binom{n}{k} = \binom{n}{0} + \binom{n}{1} + \dots + \binom{n}{n}$$

10.6 Exercises

1. $\frac{3}{5}$ 3. $\frac{9}{13}$
5. $\frac{1}{3}$
7. a. 0 b. $\frac{5}{8}$
9. a. 0 b. $\frac{3}{5}$
11. a. 0 b. 1

$$13. \text{ a. } \frac{1}{8} \quad \text{ b. } \frac{9}{16}$$

15. The set of all ordered 4-tuples made up of H's and T's. There are 16 such 4-tuples.

17. The set of all ordered pairs that have either an H or a T in the first slot and one of the 13 hearts in the second slot. There are 26 such ordered pairs.

19. The set of all ordered triples with any of the 6 values in each slot. There are 216 such triples.

21. The set of the 38 pockets.

$$23. \text{ a. } \frac{2}{3} \quad \text{ b. } \frac{1}{3}$$

$$25. \text{ a. } \frac{3}{8} \quad \text{ b. } \frac{1}{8} \quad \text{ c. } \frac{1}{2}$$

$$27. \frac{3}{10}$$

$$29. \frac{387,420,489}{1,000,000,000} \approx 0.3874$$

$$31. \frac{3}{8}$$

$$33. \text{ a. } \frac{11}{26} \quad \text{ b. } \frac{9}{52} \quad \text{ c. } \frac{2}{13}$$

$$35. \text{ a. } \frac{1}{169} \quad \text{ b. } \frac{1}{221}$$

37. 18.75%

$$39. \text{ a. } \frac{1}{6} \quad \text{ b. } \frac{5}{18} \quad \text{ c. } \frac{1}{9}$$

$$41. \frac{1}{20} \quad 43. \frac{2}{9} \quad 45. \frac{3}{10}$$

47. 27 tickets

Chapter 10 Project

$$1. \text{ a. } \frac{9}{19} \quad \text{ b. } \frac{9}{19} \quad \text{ c. } \frac{1}{38}$$

$$\text{ d. } \frac{3}{38} \quad \text{ e. } \frac{1}{38}$$

3. Approximately $-\$0.05$ (or the person betting will lose about 5 cents per play on average)

Chapter 10 Review Exercises

1. $-3, 9, -27, 81, -243$
 3. $-3, -4, -5, -6, -7$
 5. $a_n = 6n - 13$ 7. $a_n = n^2 - 1$
 9. $a_1 = -2, a_n = n(a_{n-1})$ for $n \geq 2$
 11. $-3 - 5 - 7 - 9 - 11 - 13 = -48$
 13. $\sum_{i=2}^7 i^3 = 783$
 15. $-8 - 16 - 32 - 64 - 128 = -248$
 17. $S_n = \frac{n}{2(n+2)}, S_{80} = \frac{20}{41}$
 19. $S_n = 3 - 3^{n+1}$, series diverges
 21. $-10, -12, -22, -34, -56$
 23. $a_n = \frac{5}{2}n + 9$
 25. $a_n = 3n - 1$ 27. $a_n = 9n - 14$
 29. 275 31. a_{36} 33. 8827
 35. 66
 37. $a_n = 3\left(\frac{1}{5}\right)^{n-1}$
 39. $a_n = 6(4)^{n-1}$
 41. $a_n = 8\left(\frac{1}{4}\right)^{n-1}$
 43. $r = \pm \frac{2}{3}; \pm \frac{45}{8}, \frac{15}{4}, \pm \frac{5}{2}, \frac{5}{3}, \pm \frac{10}{9}$
45. -2 47. $\frac{381}{512}$ 49. -12
 51. 1
 53.
 Basic Step: $n = 1, (3(1) + 2) = 5$
 and $\frac{1(3(1) + 7)}{2} = 5$;
 Induction Step:
 If $5 + 8 + 11 + \dots + (3k + 2) = \frac{k(3k + 7)}{2}$,
 then
 $5 + 8 + 11 + \dots + (3k + 2) + (3(k + 1) + 2)$
 $= \frac{k(3k + 7)}{2} + (3k + 5)$
 $= \frac{3k^2 + 7k + 6k + 10}{2}$
 $= \frac{(k + 1)(3k + 10)}{2}$
 $= \frac{(k + 1)(3(k + 1) + 7)}{2}$
55. Basic Step: $n = 1, 11^1 - 7^1 = 4$,
 which is divisible by 4;
 Induction Step:
 If $\frac{11^k - 7^k}{4} = p$ or $11^k - 7^k = 4p$
 for some integer p , then
 $11^{k+1} - 7^{k+1} = 11 \cdot 11^k - 7 \cdot 7^k$
 $= 4 \cdot 11^k + 7 \cdot 11^k - 7 \cdot 7^k$
 $= 4 \cdot 11^k + 7(11^k - 7^k)$
 $= 4 \cdot 11^k + 7(4p) = 4(11^k + 7p)$
57. $8 \cdot 10^3 \cdot 26^3 = 140,608,000$
 59. $\frac{8!}{3!2!} = 3360$
 61. ${}_{21}P_5 = 2,441,880$
 63. $-32y^5 + 80y^4 - 80y^3$
 $+ 40y^2 - 10y + 1$
 65. $3125x^{10} - 6250x^8y + 5000x^6y^2$
 $- 2000x^4y^3 + 400x^2y^4 - 32y^5$
 67. a. $\frac{1}{9}$ b. $\frac{2}{3}$
 69. a. $\frac{2}{7}$ b. $\frac{4}{7}$
 71. a. $\frac{1}{10}$ b. $\frac{4}{5}$
 73. $\frac{33}{108,290}$